

Cambridge International Examinations

Cambridge International Advanced Subsidiary and Advanced Level

Additional Mater	rials:	List of Form	nulae (MF9)				
Candidates answ	wer on th	e Question F	Paper.				
					1 hou	ır 45 mi	inutes
Paper 1 Pure M	lathemati	cs 1 (P1)			Ma	ay/June	e 2017
MATHEMATICS	;					97	09/13
NUMBER				NUMBER			
CENTRE				CANDIDATE			
CANDIDATE NAME							

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 75.



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2

i)	Show that $S = 2 - r$.
i)	Find the set of possible values that S can take.

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$$\overrightarrow{OA} = \begin{pmatrix} 5\\1\\3 \end{pmatrix}$$
 and $\overrightarrow{OB} = \begin{pmatrix} 5\\4\\-3 \end{pmatrix}$.

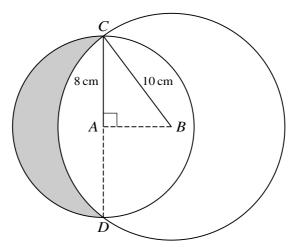
The point *P* lies on *AB* and is such that $\overrightarrow{AP} = \frac{1}{3}\overrightarrow{AB}$.

(i)	Find the position vector of P .	[3]
		•••••
(ii)	Find the distance <i>OP</i> .	[1]
(iii)	Determine whether OP is perpendicular to AB . Justify your answer.	[2]

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···	TT 1 41 41	$2\sin\theta + \cos\theta$	24 06 00 00 1000	[2]
(11)	Hence solve the equation	$\frac{1}{\sin\theta + \cos\theta} =$	$= 2 \tan \theta$ for $0^{\circ} < \theta < 180^{\circ}$.	[3]
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The diagram shows two circles with centres A and B having radii 8 cm and 10 cm respectively. The two circles intersect at C and D where CAD is a straight line and AB is perpendicular to CD.

(i)	Find angle <i>ABC</i> in radians. [1]
ii)	Find the area of the shaded region. [6]

Find an exp	pression for b	in terms of a.			
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	is a third point	such that $AP =$: AB. Calculate	the coordinates	s of the possible p
B(10, -1) of P.	is a third point	such that $AP =$: AB. Calculate	the coordinates	s of the possible p
	is a third point	such that AP =	: AB. Calculate	the coordinates	s of the possible p
	is a third point	such that AP =	AB. Calculate	the coordinates	s of the possible p
					s of the possible p

The	function f is defined by $f(x) = 9x^2 - 6x + 6$ for $x \ge p$, where p is a constant.
	State the smallest value of <i>p</i> for which f is a one-one function.
(11)	State the smallest value of p for which i is a one-one function.

(iii)	For this value of p , obtain an expression for $f^{-1}(x)$, and state the domain of f^{-1} .	[4]
		••••••
(iv)	State the set of values of q for which the equation $f(x) = q$ has no solution.	[1]

10 (a)

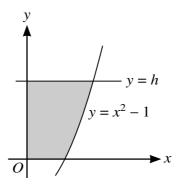


Fig. 1

Fig. 1 shows part of the curve $y = x^2 - 1$ and the line y = h, where h is a constant.

(i)	The shaded region is rotated through 360° about the y-axis . Show that the volume of revolution, V , is given by $V = \pi(\frac{1}{2}h^2 + h)$. [3]
(ii)	Find, showing all necessary working, the area of the shaded region when $h = 3$. [4]

(b)	h
	Fig. 2
	Fig. 2 shows a cross-section of a bowl containing water. When the height of the water level is $h \text{cm}$, the volume, $V \text{cm}^3$, of water is given by $V = \pi \left(\frac{1}{2}h^2 + h\right)$. Water is poured into the bowl at a constant rate of $2 \text{cm}^3 \text{s}^{-1}$. Find the rate, in $\text{cm} \text{s}^{-1}$, at which the height of the water level is increasing when the height of the water level is 3cm . [4]
	Fig. 2 shows a cross-section of a bowl containing water. When the height of the water level is $h \text{cm}$, the volume, $V \text{cm}^3$, of water is given by $V = \pi \left(\frac{1}{2}h^2 + h\right)$. Water is poured into the bowl at a constant rate of $2 \text{cm}^3 \text{s}^{-1}$. Find the rate, in cm s ⁻¹ , at which the height of the water level is
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/ .	Find $f'(x)$.		
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	Find the value of $f(0)$.		
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