

Cambridge International Examinations Cambridge International Advanced Level

	CANDIDATE NAME		
* 5 4	CENTRE NUMBER		CANDIDATE NUMBER
6 2	MATHEMATICS	3	9709/32
3 7	Paper 3 Pure M	Nathematics 3 (P3)	October/November 2017
5 7			1 hour 45 minutes
2 6	Candidates ans	wer on the Question Paper.	
*	Additional Mater	rials: List of Formulae (MF9)	
	READ THESE I	INSTRUCTIONS FIRST	

Write your Centre number, candidate number and name in the spaces at the top of this page. Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs. Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question. The total number of marks for this paper is 75.

This document consists of 19 printed pages and 1 blank page.





The diagram shows a sketch of the curve $y = \frac{3}{\sqrt{9-x^3}}$ for values of x from -1.2 to 1.2.

(i) Use the trapezium rule, with two intervals, to estimate the value of

$$\int_{-1.2}^{1.2} \frac{3}{\sqrt{9-x^3}} \, \mathrm{d}x,$$

correct to 3 significant figures.		I
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4	The curve	with equation $y =$	$\frac{2-\sin x}{\cos x}$	has one stati	onary point in	the interval –	$\frac{1}{2}\pi < x < \frac{1}{2}\pi.$	
	(i) Find	the exact coordina	tes of this	point.				[5]
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(ii)	Determine whether this point is a maximum or a minimum point.	[2]

5 The variables *x* and *y* satisfy the differential equation

$$(x+1)\frac{\mathrm{d}y}{\mathrm{d}x} = y(x+2),$$

and it is given that y = 2 when x = 1. Solve the differential equation and obtain an expression for y in terms of x. [7]

.....

6 The equation of a curve is $x^3y - 3xy^3 = 2a^4$, where *a* is a non-zero constant.

(i) Show that
$$\frac{dy}{dx} = \frac{3x^2y - 3y^3}{9xy^2 - x^3}$$
. [4]

(ii) Hence show that there are only two points on the curve at which the tangent is parallel to the x-axis and find the coordinates of these points. [4]

Th	roughout this question the use of a calculator is not permitted.	
The	e complex number $1 - (\sqrt{3})i$ is denoted by <i>u</i> .	
(i)) Find the modulus and argument of u .	
(ii)	() Show that $u^3 + 8 = 0$.	
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(iii) On a sketch of an Argand diagram, shade the region whose points represent complex numbers z satisfying both the inequalities $|z - u| \le 2$ and $\text{Re } z \ge 2$, where Re z denotes the real part of z.

[4]

8	Let $f(x) = \frac{8x^2 + 9x + 8}{(1 - x)(2x + 3)^2}$.	
	(i) Express $f(x)$ in partial fractions.	[5]

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9 It is given that
$$\int_{1}^{a} x^{\frac{1}{2}} \ln x \, dx = 2$$
, where $a > 1$.
(i) Show that $a^{\frac{3}{2}} = \frac{7 + 2a^{\frac{3}{2}}}{3 \ln a}$. [5]

(ii) Show by calculation that *a* lies between 2 and 4.

(iii) Use the iterative formula

$$a_{n+1} = \left(\frac{7 + 2a_n^{\frac{3}{2}}}{3\ln a_n}\right)^{\frac{2}{3}}$$

to determine a correct to 3 decimal places. Give the result of each iteration to 5 decimal places. [3]

[2]

(i)	
	Calculate the acute angle between the planes p and q . [4]
ii)	The point A on the line of interpreting of a and a basic accordingte equal to 2. Find the equation
	The point <i>A</i> on the line of intersection of <i>p</i> and <i>q</i> has <i>y</i> -coordinate equal to 2. Find the equation of the plane which contains the point <i>A</i> and is perpendicular to both the planes <i>p</i> and <i>q</i> . Give your answer in the form $ax + by + cz = d$.
	of the plane which contains the point A and is perpendicular to both the planes p and q . Give
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