

Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

MATHEMATICS 9709/13

Paper 1 Pure Mathematics 1

May/June 2021

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has 20 pages. Any blank pages are indicated.

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Find $f(x)$.							
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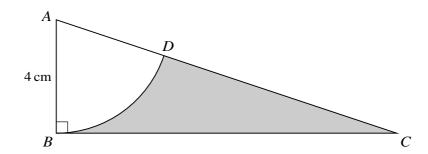
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4	(a)	Charr	that the	e equation
4	(a)	SHOW	mai me	: eauauon

$$\frac{\tan x + \sin x}{\tan x - \sin x} = k,$$

	where k is a constant, may be expressed as
	$\frac{1+\cos x}{1-\cos x} = k. ag{2}$
(b)	Hence express $\cos x$ in terms of k . [2]
(c)	Hence solve the equation $\frac{\tan x + \sin x}{\tan x - \sin x} = 4 \text{ for } -\pi < x < \pi.$ [2]

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The diagram shows a triangle ABC, in which angle $ABC = 90^{\circ}$ and AB = 4 cm. The sector ABD is part of a circle with centre A. The area of the sector is 10 cm^2 .

(a)	Find angle <i>BAD</i> in radians.	[2]
(b)	Find the perimeter of the shaded region.	[4]

6 Functions f and g are both defined for $x \in \mathbb{R}$	and are	given b	Эy
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$$f(x) = x^2 - 2x + 5,$$

$$g(x) = x^2 + 4x + 13.$$

(a)	By first expressing each of $f(x)$ and $g(x)$ in completed square form, express $g(x)$ in the form $f(x+p)+q$, where p and q are constants.
(b)	Describe fully the transformation which transforms the graph of $y = f(x)$ to the graph of $y = g(x)$

7	(a)	Write down the first four terms of the expansion, in ascending powers of x , of $(a-x)^6$. [2]
	(b)	Given that the coefficient of x^2 in the expansion of $\left(1 + \frac{2}{ax}\right)(a-x)^6$ is -20 , find in exact form
		the possible values of the constant a . [5]

8 Functions f and g are defined as follows:

f:
$$x \mapsto x^2 - 1$$
 for $x < 0$,
g: $x \mapsto \frac{1}{2x+1}$ for $x < -\frac{1}{2}$.

Solve the equation $fg(x) = 3$.	[4]

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)	Find an expression for $(fg)^{-1}(x)$.	
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Find the possible values of the common ratio.	
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(b) An arithmetic progression P has first term a and common difference d. An arithmetic progression

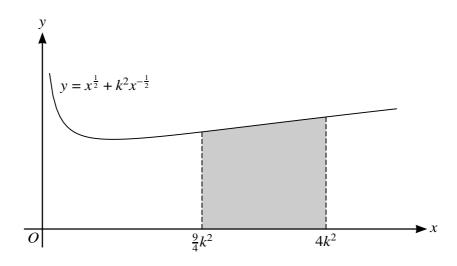
	$\frac{5\text{th term of }P}{12\text{th term of }Q}$	$=\frac{1}{3}$ and	Sum of first	$\frac{5 \text{ terms of } P}{5 \text{ terms of } Q} =$	$\frac{2}{3}$.
Find the val	ue of a and the v	value of d .			
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10	1 011	ats $A(-2, 3)$, $B(3, 0)$ and $C(6, 5)$ lie on the circumference of a circle with centre D .			
	(a)	Show that angle $ABC = 90^{\circ}$.	[2]		
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	(b)	Hence state the coordinates of D .	[1]		
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	(c)	Find an equation of the circle.	[2]		
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The point E lies on the circumference of the circle such that BE is a diameter. (d) Find an equation of the tangent to the circle at E.

l)	Find an equation of the tangent to the circle at E .	[5]

11



The diagram shows part of the curve with equation $y = x^{\frac{1}{2}} + k^2 x^{-\frac{1}{2}}$, where k is a positive constant.

(a)	Find the coordinates of the minimum point of the curve, giving your answer in terms of k . [4]

The tangent at the point on the curve where $x = 4k^2$ intersects the y-axis at P. [4] (b) Find the y-coordinate of P in terms of k. The shaded region is bounded by the curve, the x-axis and the lines $x = \frac{9}{4}k^2$ and $x = 4k^2$. (c) Find the area of the shaded region in terms of k. [3]

Additional Page

If you use the following lined page to complete the answer(s) to any question(s), the question number(s must be clearly shown.		

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