

Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

MATHEMATICS 9709/32

Paper 3 Pure Mathematics 3

October/November 2022

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

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4 (a	Express $4\cos x - \sin x$ in the form $R\cos(x + \alpha)$, where $R > 0$ and $0^{\circ} < \alpha < 90^{\circ}$ value of R and give α correct to 2 decimal places.	State the exact [3]
(l	Hence solve the equation $4\cos 2x - \sin 2x = 3$ for $0^{\circ} < x < 180^{\circ}$.	[5]

5	(a)	Solve the equation $z^2 - 6iz - 12 = 0$, giving the answers in the form $x + iy$, where x and y are real and exact. [3]
	(1.)	

(b) On a sketch of an Argand diagram with origin O, show points A and B representing the roots of the equation in part (a). [1]

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Hence show that the triangle OAB is equilateral.	
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Hence show that the triangle OAB is equilateral.	
Hence show that the triangle <i>OAB</i> is equilateral.	

6	Relative to	the origin O ,	the points A ,	B and C have	position v	ectors given	by

n
$$O$$
, the points A , B and C have position vectors give.
$$\overrightarrow{OA} = \begin{pmatrix} 1 \\ 3 \\ 1 \end{pmatrix}, \quad \overrightarrow{OB} = \begin{pmatrix} 3 \\ 1 \\ 2 \end{pmatrix} \quad \text{and} \quad \overrightarrow{OC} = \begin{pmatrix} 5 \\ 3 \\ -2 \end{pmatrix}.$$

Using a scalar product, find the cosine of angle <i>BAC</i> .	[4]

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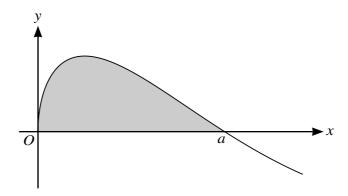
7	The variables	x and θ	9 satisfy	the differe	ntial equation
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$$x\sin^2\theta \frac{\mathrm{d}x}{\mathrm{d}\theta} = \tan^2\theta - 2\cot\theta,$$

for $0 < \theta < \frac{1}{2}\pi$ and x > 0. It is given that x = 2 when $\theta = \frac{1}{4}\pi$.

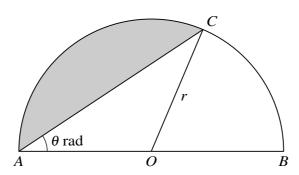
(-)	$d_{(-1)}$	$2 \cot \theta$
(a)	Show that $\frac{d}{d\theta}(\cot^2\theta) =$	$-\frac{1}{\sin^2\theta}$

							$\operatorname{osec}^2 \theta$.)
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Solve the v				value of x wh			



The diagram shows part of the curve $y = \sin \sqrt{x}$. This part of the curve intersects the *x*-axis at the point where x = a.

(a)	State the exact value of a .	[1]
(b)	Using the substitution $u = \sqrt{x}$, find the exact area of the shaded region in the bounded by this part of the curve and the x-axis.	first quadrant [7]
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The diagram shows a semicircle with diameter AB, centre O and radius r. The shaded region is the minor segment on the chord AC and its area is one third of the area of the semicircle. The angle CAB is θ radians.

(a)	Show that $\theta = \frac{1}{3}(\pi - 1.5\sin 2\theta)$.	[4]
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10	Let $f(x) =$	$4 - x + x^2$	
10	Let $I(x) =$	$(1+x)(2+x^2)$.	

(a)	Express $f(x)$ in partial fractions.	[5]

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Additional Page

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