

# Cambridge International AS & A Level

CANDIDATE NAME		
CENTRE NUMBER		CANDIDATE NUMBER
MATHEMATI	cs	9709/11
Paper 1 Pure N	Nathematics 1	May/June 2023
		1 hour 50 minutes
You must answ	ver on the question paper.	

You will need: List of formulae (MF19)

## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.

This document has 20 pages. Any blank pages are indicated.

• Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

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2	(a)	Find the first three terms in the expansion, in ascending powers of x, of $(2 + 3x)^4$ .	[2]
	( <b>b</b> )	Find the first three terms in the expansion, in ascending powers of x, of $(1 - 2x)^5$ .	[2]
	(0)	The the first three terms in the expansion, in ascending powers of x, of $(1 - 2x)$ .	
			•••••
	(c)	Hence find the coefficient of $x^2$ in the expansion of $(2 + 3x)^4(1 - 2x)^5$ .	[2]
			•••••
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4

The diagram shows graphs with equations y = f(x) and y = g(x).

Describe fully a sequence of two transformations which transforms the graph of y = f(x) to y = g(x). [4]




The diagram shows a sector *ABC* of a circle with centre *A* and radius 8 cm. The area of the sector is  $\frac{16}{3}\pi$  cm<sup>2</sup>. The point *D* lies on the arc *BC*.

Find the perimeter of the segment BCD. [4] ..... ..... ..... .....

4

5 The line with equation y = kx - k, where k is a positive constant, is a tangent to the curve with equation  $y = -\frac{1}{2x}$ .

Find, in either order, the value of k and the coordinates of the point where the tangent meets the curve. [5]

..... ..... ..... ..... ..... ..... ..... ..... ..... ..... ..... ..... ..... ..... ..... .....

- 6 The first three terms of an arithmetic progression are  $\frac{p^2}{6}$ , 2p 6 and p.
  - (a) Given that the common difference of the progression is not zero, find the value of p. [3]

..... ..... ..... ..... ..... ..... ..... ..... ..... ..... (b) Using this value, find the sum to infinity of the geometric progression with first two terms  $\frac{p^2}{6}$  and 2p-6. [2] ..... ..... .....

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..... ..... ..... (**b**) Sketch the curve. [2] y ► x 2π 3π 4π 0 π (c) State the number of solutions of the equation  $2 + 3\sin\frac{1}{2}x = 5 - 2x$ for  $0 \le x \le 4\pi$ . [1] 

A curve has equation  $y = 2 + 3 \sin \frac{1}{2}x$  for  $0 \le x \le 4\pi$ .

(a) State greatest and least values of *y*.

7

.....

### [Turn over

[2]

## 8 The functions f and g are defined as follows, where *a* and *b* are constants.

$$f(x) = 1 + \frac{2a}{x-a} \text{ for } x > a$$
$$g(x) = bx - 2 \text{ for } x \in \mathbb{R}$$

Given that $f(7) = \frac{5}{2}$ and $gf(5) = 4$ , find the values of <i>a</i> and <i>b</i> .	
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For the rest of this question, you should use the value of *a* which you found in (a). (**b**) Find the domain of  $f^{-1}$ . [1] ..... ..... ..... ..... ..... ..... (c) Find an expression for  $f^{-1}(x)$ . [3] ..... ..... ..... ..... ..... ..... ..... ..... ..... ..... ..... .....

9 Water is poured into a tank at a constant rate of  $500 \text{ cm}^3$  per second. The depth of water in the tank, t seconds after filling starts, is h cm. When the depth of water in the tank is h cm, the volume,  $V \text{ cm}^3$ , of water in the tank is given by the formula  $V = \frac{4}{3}(25 + h)^3 - \frac{62500}{3}$ .

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F	Find the value of $V$ at this instant.	
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The diagram shows part of the curve with equation  $y = \frac{4}{(2x-1)^2}$  and parts of the lines x = 1 and y = 1. The curve passes through the points A(1, 4) and  $B, (\frac{3}{2}, 1)$ .

(a) Find the exact volume generated when the shaded region is rotated through  $360^{\circ}$  about the *x*-axis. [5]

 (b) A triangle is formed from the tangent to the curve at B, the normal to the curve at B and the *x*-axis.

Find the area of this triangle.	[6]

11	The has	equation of a curve is such that $\frac{dy}{dx} = 6x^2 - 30x + 6a$ , where <i>a</i> is a positive constant. The curve a stationary point at $(a, -15)$ .
	<b>(a)</b>	Find the value of <i>a</i> . [2]
	(b)	Determine the nature of this stationary point. [2]

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(c)	Find the equation of the curve.	[3]
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		[0]
(d)	Find the coordinates of any other stationary points on the curve.	[2]
		•••••••••••••••••••••••••••••••••••••••

y

0

A

► x

Q

Р

poin	diagram shows a circle P with centre (0, 2) and radius 10 and the tangent to the circle at the t A with coordinates (6, 10). It also shows a second circle Q with centre at the point where this ent meets the y-axis and with radius $\frac{5}{2}\sqrt{5}$ .	
<b>(a)</b>	Write down the equation of circle <i>P</i> . [1]	]
		•
		•
		•
(b)	Find the equation of the tangent to the circle $P$ at $A$ . [2]	]
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intersection of the two circles are 11. [3] ..... ..... ..... ..... ..... ..... ..... ..... ..... ..... (d) Find the coordinates of the points of intersection of the tangent and circle Q, giving the answers in surd form. [3] ..... ..... ..... ..... ..... .....

(c) Find the equation of circle Q and hence verify that the y-coordinates of both of the points of

## **Additional Page**

If you use the following lined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.

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