

## Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

MATHEMATICS 9709/13

Paper 1 Pure Mathematics 1

May/June 2023

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

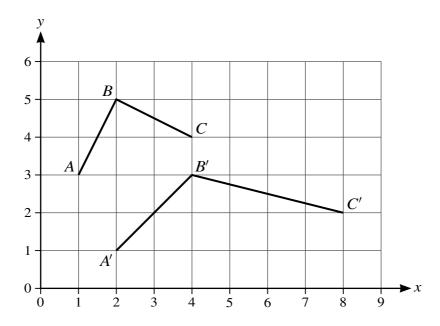
## **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

## **INFORMATION**

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages.



The diagram shows the graph of y = f(x), which consists of the two straight lines AB and BC. The lines A'B' and B'C' form the graph of y = g(x), which is the result of applying a sequence of two transformations, in either order, to y = f(x).

State fully the two transformations.	[4]

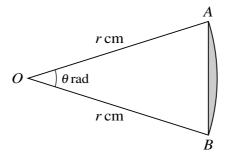

3	(a)	Give the complete expansion of $\left(x + \frac{2}{x}\right)^5$ .	[2]
	<b>(b)</b>	In the expansion of $(a + bx^2)\left(x + \frac{2}{x}\right)^5$ , the coefficient of x is zero and the coeff	Sicient of $\frac{1}{x}$ is 80.
		Find the values of the constants $a$ and $b$ .	[4]
		Find the values of the constants a and b.	
		Find the values of the constants a and b.	
		Find the values of the constants a and b.	[4]
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4 (a) Show that the equation	tion
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		. 2		_
Hence solve the equ	uation $3 \tan^2 x - 3$	$\sin^2 x - 4 = 0 \text{ for}$	$0^{\circ} \leqslant x \leqslant 180^{\circ}$ .	[4
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	(a)	Find the coordinates of the two points of intersection. [4
b) Find an equation of the circle with diameter AB.		
Find an equation of the circle with diameter AB.		
	<b>b</b> )	Find an equation of the circle with diameter $AB$ . [3]



The diagram shows a sector OAB of a circle with centre O and radius r cm. Angle  $AOB = \theta$  radians. It is given that the length of the arc AB is 9.6 cm and that the area of the sector OAB is 76.8 cm<sup>2</sup>.

(a)	Find the area of the shaded region.	[5]
<b>(b)</b>	Find the perimeter of the shaded region.	[2]

The	function f is defined by $f(x) = 2 - \frac{5}{x+2}$ for $x > -2$ .	
	State the range of f.	[1
		· • • • •
<b>(b)</b>	Obtain an expression for $f^{-1}(x)$ and state the domain of $f^{-1}$ .	[4]
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The function g is defined by g(x) = x + 3 for x > 0.

(c)	Obtain an expression for $fg(x)$ giving your answer in the form integers.	$\frac{ax+b}{cx+d}$ , where a, b, c and d are

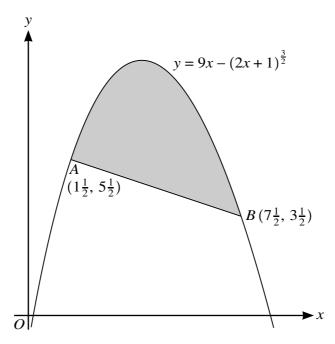
A p	ogression has first term a and second term $\frac{a^2}{a+2}$ , where a is a positive constant.						
(a)	For the case where the progression is geometric and the sum to infinity is 264, find the value of $a$ .						

for the sum of the first $n$ terms to be less than $-480$ .	
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	arve which passes through (0, 3) has equation $y = f(x)$ . It is given that $f'(x) = 1 - \frac{2}{(x-1)^3}$ . Find the equation of the curve.

The tangent to the curve at (0, 3) intersects the curve again at one other point, P.

( <b>b</b> )	Show that the x-coordinate of P satisfies the equation $(2x+1)(x-1)^2 - 1 = 0$ .	[4]
(c)	Verify that $x = \frac{3}{2}$ satisfies this equation and hence find the y-coordinate of $P$ .	[2]
		•••••



The diagram shows the points  $A\left(1\frac{1}{2}, 5\frac{1}{2}\right)$  and  $B\left(7\frac{1}{2}, 3\frac{1}{2}\right)$  lying on the curve with equation  $y = 9x - (2x+1)^{\frac{3}{2}}$ .

(a)	Find the coordinates of the maximum point of the curve. [4]

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]	Find the area of the shaded region.
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## **Additional Page**

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