



Cambridge International AS & A Level

MATHEMATICS

9709/51

Paper 5 Probability & Statistics 1

October/November 2023

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2023 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

This document consists of **18** printed pages.

PUBLISHED**Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

PUBLISHED**Mark Scheme Notes**

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
 - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
 - The total number of marks available for each question is shown at the bottom of the Marks column.
 - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
 - Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

Abbreviations

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

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Question	Answer	Marks	Guidance
1(a)	[IQR =] 31 – 23.7	M1	30.5 < UQ < 31.25 – 23.25 < LQ ≤ 24 Evidence of graph use must be seen at least once.
	7.3	A1	7.0 ≤ IQR ≤ 7.5 If M0 scored, SC B1 for 7.0 ≤ IQR ≤ 7.5 www.
		2	
1(b)	[65% of 120 =]78	B1	Seen or implied by use on graph.
	28.5	B1	28 < ans < 29
		2	

Question	Answer	Marks	Guidance
2(a)	$\left(\frac{21}{36}\right)^4 \left(\frac{15}{36}\right)$	M1	$(1-p)^4 \times p, 0 < p < 1$
	$= \frac{12005}{248832}, 0.0482$	A1	0.0482454... to at least 3SF.
		2	

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Question	Answer	Marks	Guidance
2(b)	Method 1		
	$[P(X \leq 4) =] 1 - \left(\frac{21}{36}\right)^4$	M1	$1 - b^r$, $b = \text{their } (1 - p)$ in 2(a) or correct; $r = 4, 5$.
	$= \frac{18335}{20736}, 0.884$	A1	0.884211... to at least 3SF.
		2	
	Method 2		
	$[P(X \leq 4) =] \frac{15}{36} + \frac{15}{36} \times \frac{21}{36} + \frac{15}{36} \times \left(\frac{21}{36}\right)^2 + \frac{15}{36} \times \left(\frac{21}{36}\right)^3$	M1	$p + p(1 - p) + p(1 - p)^2 + p(1 - p)^3$ [$+ p(1 - p)^4$] FT from 2(a) or correct.
	$= \frac{18335}{20736}, 0.884$	A1	0.884211... to at least 3SF.
		2	

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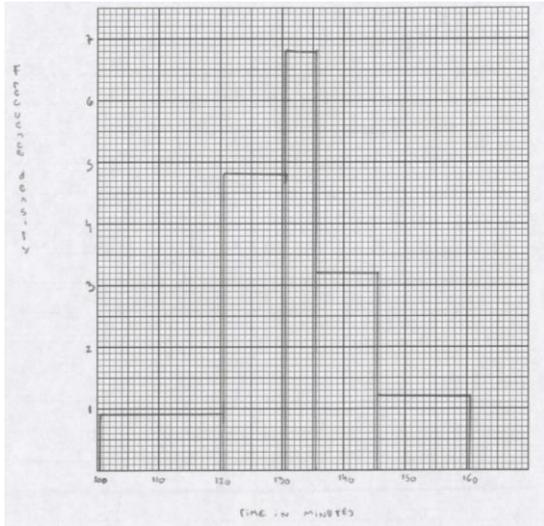
Question	Answer	Marks	Guidance
2(c)	Method 1		
	$[P(0,1,2) =] {}^8C_0 \left(\frac{5}{12}\right)^0 \left(\frac{7}{12}\right)^8 + {}^8C_1 \left(\frac{5}{12}\right)^1 \left(\frac{7}{12}\right)^7 + {}^8C_2 \left(\frac{5}{12}\right)^2 \left(\frac{7}{12}\right)^6$	M1	One term ${}^8C_x (q)^x (1-q)^{8-x}$, $0 < q < 1$, $x \neq 0, 8$.
	$0.01341 + 0.07661 + 0.1915$	A1 FT	Correct expression, accept unsimplified, no terms omitted leading to final answer. FT only with unsimplified expression.
	= 0.282	B1	$0.2815 \leq q \leq 0.282$
	Method 2		
	$[1 - P(3,4,5,6,7,8) =] 1 - ({}^8C_3 \left(\frac{5}{12}\right)^3 \left(\frac{7}{12}\right)^5 + {}^8C_4 \left(\frac{5}{12}\right)^4 \left(\frac{7}{12}\right)^4 + \dots + {}^8C_7 \left(\frac{5}{12}\right)^7 \left(\frac{7}{12}\right)^1 + {}^8C_8 \left(\frac{5}{12}\right)^8 \left(\frac{7}{12}\right)^0)$ $= 1 - (0.2736 + 0.2443 + \dots + 0.01017 + 9.084 \times 10^{-4})$	M1	One term ${}^8C_x (q)^x (1-q)^{8-x}$, $0 < q < 1$, $x \neq 0, 8$.
		A1 FT	Correct expression, accept unsimplified, no terms omitted leading to final answer. FT only with unsimplified expression.
	= 0.282	B1	$0.2815 \leq q \leq 0.282$
		3	

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Question	Answer	Marks	Guidance
3(a)	$[P(X < 76) =] P\left(Z < \frac{76 - 80.5}{6.6}\right)$	M1	Use of \pm standardisation formula with 76, 80.5 and 6.6, condone 6.6^2 or $\sqrt{6.6}$, no continuity correction.
	$[= \Phi(-0.6818) = 1 - \Phi(0.6818) =]$ $1 - 0.7524 = 0.2476$	M1	Calculating the appropriate probability area (leading to their final answer).
	24.8%	A1	24.75% < ans \leq 24.8% (percentage value required). If A0 scored, SC B1 for 24.75% < ans \leq 24.8% www.
		3	
3(b)	$[\% \text{ of large eggs} = 100 - 40 - 24.76 = 35.24]$ $[P\left(Z > \frac{x - 80.5}{6.6}\right) = 0.40 + 0.2476 = 0.6476]$ $\frac{x - 80.5}{6.6} = 0.378$	B1	$0.378 \leq z < 0.3791$ or $-0.3791 < z \leq -0.378$ seen.
		M1	Use of \pm standardisation formula with x , 80.5, 6.6 and a z -value (not 0.6476, 0.3524, 0.4, 0.2476) (treat ± 0.38 as a z -value), not 6.6^2 , not $\sqrt{6.6}$, no continuity correction.
	$x = 83[.0]$	A1	awrt 83.0
		3	

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Question	Answer	Marks	Guidance
3(c)	Mean = $150 \times 0.4 = 60$ Var = $150 \times 0.4 \times 0.6 = 36$	B1	60 and 36 seen, allow unsimplified.
	$P(X > 68) = P\left(Z > \frac{68.5 - 60}{\sqrt{36}}\right)$	M1	Substituting <i>their</i> 60 and <i>their</i> 6 into \pm standardisation formula (any number for 68.5), condone <i>their</i> σ^2 and <i>their</i> $\sqrt{\sigma}$.
		M1	Using continuity correction 67.5 or 68.5 in <i>their</i> standardisation formula.
	$P(Z > 1.417) = 1 - \Phi(1.417)$ [= $1 - 0.9217$]	M1	Appropriate area Φ , from final process, must be a probability.
	0.0783	A1	$0.07825 < p \leq 0.0783$ If A0 scored, SC B1 for $0.07825 < p \leq 0.0783$.
		5	

Question	Answer						Marks	Guidance							
4(a)	<table border="1"> <tr> <td>Class width</td> <td>20</td> <td>10</td> <td>5</td> <td>10</td> <td>15</td> </tr> <tr> <td>Frequency density</td> <td>0.9</td> <td>4.8</td> <td>6.8</td> <td>3.2</td> <td>1.2</td> </tr> </table>	Class width	20	10	5	10	15	Frequency density	0.9	4.8	6.8	3.2	1.2	M1	At least 4 frequency densities calculated by $\frac{f}{cw}$ e.g. $\frac{18}{20}$ (condone $\frac{f}{cw \pm 0.5}$ if unsimplified). Accept unsimplified, may be read from graph using <i>their</i> scale, no lower than 1cm = 1 fd.
Class width	20	10	5	10	15										
Frequency density	0.9	4.8	6.8	3.2	1.2										
		A1	All bar heights correct on graph (no FT), using their suitable linear scale with at least 3 values indicated, no lower than 1cm = 1 fd.												
		B1	Bar ends at 120.5, 130.5, 135.5, 145.5, 160.5. 5 bars drawn with a horizontal linear scale, no lower than 1 cm = 10 min, with at least 3 values indicated. $100 \leq \text{horizontal scale} \leq 160$.												
		B1	Axes labelled frequency density (fd), time (t) and minutes (min, m) oe, or an appropriate title. (Axes may be reversed).												
		4													

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Question	Answer	Marks	Guidance
4(b)	[Midpoints] 110.5 125.5 133 140.5 153	B1	At least 4 correct mid-points seen, may be by data table or used in formula.
	$\text{Mean} = \frac{18 \times 110.5 + 48 \times 125.5 + 34 \times 133 + 32 \times 140.5 + 18 \times 153}{150}$ $= \frac{1989 + 6024 + 4522 + 4496 + 2754}{150}$	M1	Correct formula for mean using midpoints ± 0.5 , condone 1 midpoint error within class.
	= 131.9	A1	Accept 132, $131 \frac{9}{10}$, or $\frac{1319}{10}$. Must be identified.
	$\text{Variance} = \frac{18 \times 110.5^2 + 48 \times 125.5^2 + 34 \times 133^2 + 32 \times 140.5^2 + 18 \times 153^2}{150} - (\text{their } 131.9)^2$	M1	<p>Appropriate variance formula with <i>their</i> 5 midpoints within class (not upper bound, lower bound, class width, frequency density, frequency or cumulative frequency). Condone 1 error.</p> <p>If correct midpoints seen, accept</p> $\left\{ \frac{3200 + 41400 + 194400 + 157300 + 153600}{150} \text{ or } \frac{2630272.5}{150} \right\}$ <p>–{131.9² or 17397.61}.</p>
	[= 137.54] [Standard deviation =] 11.7	A1	11.7277448... to at least 3SF. Accept $11.6 \leq \sigma < 11.95$ www. If M0 awarded, SC B1 $11.6 \leq \sigma < 11.95$ www.
		5	

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Question	Answer	Marks	Guidance																									
5(a)	$0.28 + 6p = 1, p = 0.12$	B1	Using sum of probabilities = 1 to form an equation. Accept $0.28 + p + 2p + 3p = 1, p = 0.12$. Substitution of 0.12 into the expression scores B0.																									
		1																										
5(b)	<p>[For fair spinners (blue and green), probability of any score is 0.25 Scenarios to give total 4 or less:]</p> <table border="1" data-bbox="199 480 844 911"> <thead> <tr> <th>R</th> <th>B</th> <th>G</th> <th></th> <th></th> </tr> </thead> <tbody> <tr> <td>1</td> <td>1</td> <td>2</td> <td>$0.28 \times (0.25)^2$</td> <td>= 0.0175</td> </tr> <tr> <td>1</td> <td>2</td> <td>1</td> <td>$0.28 \times (0.25)^2$</td> <td>= 0.0175</td> </tr> <tr> <td>1</td> <td>1</td> <td>1</td> <td>$0.28 \times (0.25)^2$</td> <td>= 0.0175</td> </tr> <tr> <td>2</td> <td>1</td> <td>1</td> <td>$0.12 \times (0.25)^2$</td> <td>= 0.0075</td> </tr> </tbody> </table>	R	B	G			1	1	2	$0.28 \times (0.25)^2$	= 0.0175	1	2	1	$0.28 \times (0.25)^2$	= 0.0175	1	1	1	$0.28 \times (0.25)^2$	= 0.0175	2	1	1	$0.12 \times (0.25)^2$	= 0.0075	B1	Correct probability for 1 identified scenario, accept unsimplified, www.
R	B	G																										
1	1	2	$0.28 \times (0.25)^2$	= 0.0175																								
1	2	1	$0.28 \times (0.25)^2$	= 0.0175																								
1	1	1	$0.28 \times (0.25)^2$	= 0.0175																								
2	1	1	$0.12 \times (0.25)^2$	= 0.0075																								
	0.06	A1	If A0 scored, SC B1 for 0.06 www.																									
		3																										

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Question	Answer	Marks	Guidance																																																												
5(c)	[P(X is odd) = 0.28 + 2×0.12 or 0.24]= 0.52[0]	B1	Seen alone or as the denominator of a conditional probability fraction. Accept unsimplified.																																																												
	<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 10%;">R</th> <th style="width: 10%;">B</th> <th style="width: 10%;">G</th> <th style="width: 20%;"></th> <th style="width: 10%;"></th> <th style="width: 10%;"></th> </tr> </thead> <tbody> <tr> <td>1</td> <td>1</td> <td>1</td> <td>$0.28 \times (0.25)^2$</td> <td>=</td> <td>0.0175</td> </tr> <tr> <td>1</td> <td>1</td> <td>2</td> <td>$0.28 \times (0.25)^2$</td> <td>=</td> <td>0.0175</td> </tr> <tr> <td>1</td> <td>1</td> <td>3</td> <td>$0.28 \times (0.25)^2$</td> <td>=</td> <td>0.0175</td> </tr> <tr> <td>1</td> <td>1</td> <td>4</td> <td>$0.28 \times (0.25)^2$</td> <td>=</td> <td>0.0175</td> </tr> <tr> <td>1</td> <td>2</td> <td>1</td> <td>$0.28 \times (0.25)^2$</td> <td>=</td> <td>0.0175</td> </tr> <tr> <td>1</td> <td>2</td> <td>2</td> <td>$0.28 \times (0.25)^2$</td> <td>=</td> <td>0.0175</td> </tr> <tr> <td>1</td> <td>3</td> <td>1</td> <td>$0.28 \times (0.25)^2$</td> <td>=</td> <td>0.0175</td> </tr> <tr> <td>1</td> <td>4</td> <td>1</td> <td>$0.28 \times (0.25)^2$</td> <td>=</td> <td>0.0175</td> </tr> <tr> <td>3</td> <td>1</td> <td>1</td> <td>$0.24 \times (0.25)^2$</td> <td>=</td> <td>0.015</td> </tr> </tbody> </table>	R	B	G				1	1	1	$0.28 \times (0.25)^2$	=	0.0175	1	1	2	$0.28 \times (0.25)^2$	=	0.0175	1	1	3	$0.28 \times (0.25)^2$	=	0.0175	1	1	4	$0.28 \times (0.25)^2$	=	0.0175	1	2	1	$0.28 \times (0.25)^2$	=	0.0175	1	2	2	$0.28 \times (0.25)^2$	=	0.0175	1	3	1	$0.28 \times (0.25)^2$	=	0.0175	1	4	1	$0.28 \times (0.25)^2$	=	0.0175	3	1	1	$0.24 \times (0.25)^2$	=	0.015	M1	Values of at least 5 identified correct scenarios added, accept unsimplified, condone incorrect scenarios in calculation.
R	B	G																																																													
1	1	1	$0.28 \times (0.25)^2$	=	0.0175																																																										
1	1	2	$0.28 \times (0.25)^2$	=	0.0175																																																										
1	1	3	$0.28 \times (0.25)^2$	=	0.0175																																																										
1	1	4	$0.28 \times (0.25)^2$	=	0.0175																																																										
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1	3	1	$0.28 \times (0.25)^2$	=	0.0175																																																										
1	4	1	$0.28 \times (0.25)^2$	=	0.0175																																																										
3	1	1	$0.24 \times (0.25)^2$	=	0.015																																																										
	[P(product of 3 scores $\leq 4 \cap X$ is odd) =] $0.28 \times (0.25)^2 \times 8 + 0.24 \times (0.25)^2$	M1	$0.28 \times (0.25)^2 \times x + 0.24 \times (0.25)^2$, or $0.0175 \times x + 0.015$ where $x = 4, 5, 6, 7, \text{ or } 8$. Seen alone or as numerator/denominator of a conditional probability fraction.																																																												

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Question	Answer	Marks	Guidance
5(c)	$\left[\frac{P(\text{product of 3 scores} \leq 4 \mid X \text{ is odd})}{P(X \text{ is odd})} = \right]$	M1	$\frac{0.28 \times (0.25)^2 \times x + 0.24 \times (0.25)^2}{0.28 + 0.24} \quad x = 4, 5, 6, 7, 8$ <p>or</p> $\frac{\text{their identified } P(\text{product of 3 scores is 4 or less and } X \text{ is odd})}{\text{their identified } P(\text{odd})}$
	$\frac{0.155}{0.52}$	A1	0.2980769... to at least 3SF.
	$= 0.298, \frac{155}{520}, \frac{31}{104}$	5	

Question	Answer	Marks	Guidance
6(a)	${}^5C_2 \times 2$	M1	${}^5C_2 \times r$, $r =$ positive integer, 1 implied, no addition.
		M1	$s \times 2$, $s = {}^5C_2$ or 5P_2 or if 5C_2 or 5P_2 not present, $s =$ a single integer > 1 or $t! \times 2$, $2 \leq t \leq 8$, no other terms.
	20	A1	
		3	

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Question	Answer	Marks	Guidance
6(b)	Method 1		
	${}^6C_2 \times 2 \times 2 \times 2 \times 4!$	M1	${}^6C_2 \times 2 \times 2 \times 2 \times t$, $t = \text{positive integer} \geq 1$. ${}^6P_2 \times 2 \times 2 \times t$, $t = \text{positive integer} \geq 1$.
		M1	$u \times 4!$, $u = \text{positive integer} > 1$.
	2880	A1	If A0 scored, SC B1 for 2880 nfw.
	Method 2		
	$6! \times 2 \times 2$	M1	$6! \times v$, $v = \text{positive integer} \geq 1$.
		M1	$w \times 2 \times 2$, $w = \text{positive integer} > 1$. condone $w \times 4$, $w = \text{positive integer} > 1$.
	2880	A1	If A0 scored, SC B1 for 2880 nfw.
		3	

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Question	Answer	Marks	Guidance
6(c)	Method 1: Number of arrangements with Rajid and Sue together – Number of arrangements with Rajid and Sue together and at end of line		
	$7! \times 2 - 6! \times 4$	M1	$7! \times 2 - a$, $a =$ positive integer > 1 .
		M1	$b - 6! \times 4$, $b =$ positive integer > 2880 .
		M1	$7! \times c - 6! \times d$, $c = 1, 2$ and $d = 1, 4$.
	$= 7200$	A1	If A0 scored, SC B1 for 7200 nfw.
	Method 2: Arrangements of 6 people and then place Rajid and Sue		
	$6! \times 2 \times 5$	M1	$6! \times e \times f$, $e, f =$ positive integers ≥ 1 .
		M1	$6! \times 2 \times f$, $f =$ positive integer ≥ 1 . If 5! Used, SC B1 $5! \times 2 \times f$, $f =$ positive integer > 1 .
		M1	$6! \times e \times 5$, $e =$ positive integer ≥ 1 .
	7200	A1	If A0, scored SC B1 for 7200 nfw.
	Method 3: Friends at ends picked first F ^ RS ^ ^ ^ F		
	${}^6P_2 \times 5! \times 2$	M1	${}^6P_2 \times e \times f$, $e, f =$ positive integers ≥ 1 .
		M1	${}^6P_2 \times 5! \times f$, $f =$ positive integer ≥ 1 . Condone ${}^6C_2 \times 5! \times f$, $f =$ positive integer ≥ 1 .
		M1	${}^6P_2 \times e \times 2$, $e =$ positive integer ≥ 1 . Condone ${}^6C_2 \times e \times 2$, $e =$ positive integer ≥ 1 .
7200	A1	If A0 scored, SC B1 for 7200 nfw.	

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Question	Answer	Marks	Guidance
6(c)	Method 4: RS placed in different possible positions		
	${}^6P_1 \times 2 \times 5! = 1440$ ${}^6P_2 \times 2 \times 4! = 1440$	M1	${}^6P_n \times a \times (6-n)!$, $a =$ positive integer, $1 \leq n \leq 5$ seen once.
	${}^6P_3 \times 2 \times 3! = 1440$ ${}^6P_4 \times 2 \times 2! = 1440$	M1	${}^6P_n \times 2 \times (6-n)!$, $a =$ positive integer, $1 \leq n \leq 5$ seen at least 3 times in identified scenarios.
	${}^6P_5 \times 2 \times 1! = 1440$	M1	Add 5 values of appropriate scenarios only. No additional, incorrect or repeated scenarios. Accept unsimplified.
	7200	A1	If A0 scored, SC B1 for 7200 nfw.
		4	