

# Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

MATHEMATICS

Paper 1 Pure Mathematics 1

October/November 2023

1 hour 50 minutes

9709/13

You must answer on the question paper.

You will need: List of formulae (MF19)

#### **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

#### **INFORMATION**

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

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Find the equation of the curve.	

(a)	Find the y-coordinates of $A$ and $B$ , expressing your answers in terms of surds.	I
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		••••••
<b>b</b> )	Find the equation of the circle which has $AB$ as its diameter.	
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3 (a) Show that the	equation
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$5\cos\theta$ – s	$\sin \theta \tan$	$\theta + 1$	= 0
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Hence solve the	equation 5 cos 6	$\theta - \sin \theta \tan \theta + 1 = 0$ for	$0<\theta<2\pi.$	
Hence solve the	equation 5 cos 6		$0 < \theta < 2\pi$ .	
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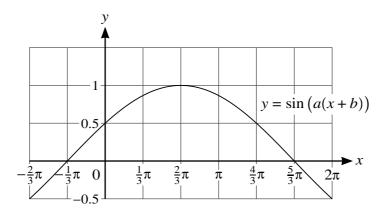
	and the following in ascending powers of $x$ up to and including the term in $x^2$ .	
<b>(i)</b> (1	$1+2x)^5.$	
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(ii) (1	$(1-ax)^6$ , where a is a constant.	
(11) (1	i awy, whole a is a constant.	
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	ansion of $(1 + 2x)^5(1 - ax)^6$ , the coefficient of $x^2$ is $-5$ . the possible values of $a$ .	•••
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1)	Find the possible values of the constant $p$ .	I
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	One of the values of $p$ found in (a) is a negative fraction.	
	One of the values of $p$ found in (a) is a negative fraction.  Use this value of $p$ to find the sum to infinity of this progression.	

Find the possi	ble values of $c$ as	nd the correspon	nding coordinates	of <i>P</i> .	[7
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	e function f is defined by $f(x) = 1 + \frac{3}{x-2}$ for $x > 2$ .	-
(a)	State the range of f.	[
<b>(b)</b>	Obtain an expression for $f^{-1}(x)$ and state the domain of $f^{-1}$ .	[4
Γhe	e function g is defined by $g(x) = 2x - 2$ for $x > 0$ .	
(c)	Obtain a simplified expression for $gf(x)$ .	[2

**(b)** 



The diagram shows part of the graph of  $y = \sin(a(x+b))$ , where a and b are positive constants.

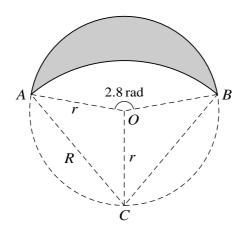
(a)	State the value of $a$ and one possible value of $b$ .	[2]
		•••••

Another curve, with equation y = f(x), has a single stationary point at the point (p, q), where p and q are constants. This curve is transformed to a curve with equation

$$y = -3f\left(\frac{1}{4}(x+8)\right).$$

For the transformed curve, find the coordinates of the stationary point, giving your answer terms of $p$ and $q$ .	r in [3]

	Find the equation of the normal to the curve at the point $A(4, 3)$ , giving your answer in the for
	y = mx + c.
	point is moving along the curve $y = 2x^{\frac{1}{2}} - 1$ in such a way that at A the rate of increase of the bordinate is $3 \mathrm{cm}\mathrm{s}^{-1}$ .
(b)	Find the rate of increase of the <i>y</i> -coordinate at <i>A</i> .
	A the moving point suddenly changes direction and speed, and moves down the normal in such that the rate of decrease of the y-coordinate is constant at $5 \mathrm{cm}\mathrm{s}^{-1}$ .
way	A the moving point suddenly changes direction and speed, and moves down the normal in such
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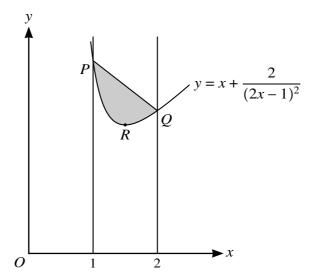


The diagram shows points A, B and C lying on a circle with centre O and radius r. Angle AOB is 2.8 radians. The shaded region is bounded by two arcs. The upper arc is part of the circle with centre O and radius r. The lower arc is part of a circle with centre C and radius R.

(a)	State the size of angle $ACO$ in radians. [1]
<b>(b)</b>	Find $R$ in terms of $r$ . [1]

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(a)



The diagram shows part of the curve with equation  $y = x + \frac{2}{(2x-1)^2}$ . The lines x = 1 and x = 2 intersect the curve at P and Q respectively and R is the stationary point on the curve.

Verify that the x-coordinate of R is $\frac{3}{2}$ and find the y-coordinate of R.	[4]
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### **Additional Page**

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