

# Cambridge International AS & A Level

CANDIDATE NAME						
CENTRE NUMBER				CANDIDATE NUMBER		

MATHEMATICS 9709/22

Paper 2 Pure Mathematics 2

October/November 2023

1 hour 15 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

#### **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

#### **INFORMATION**

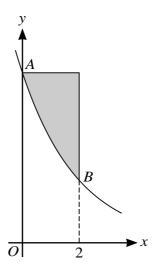
- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

1 When the	ne polynomial
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$ax^3$	_	$4ax^2$	_ 7	ı		5
ux	+	<del>4</del> ux	- /	x	_	٠,

is divided by $(x + 2)$ , the remainder is 33.	
Find the value of the constant $a$ .	[2]

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The diagram shows the curve with equation  $y = 6e^{-\frac{1}{2}x}$ . The points on the curve with x-coordinates 0 and 2 are denoted by A and B respectively. The shaded region is enclosed by the curve, the line through A parallel to the x-axis and the line through B parallel to the y-axis.

(a)	Find the exact gradient of the curve at <i>B</i> .	[2]	

Find the exact area of the shaded region.	

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4	(a)	Sketch, on the same diagram, the graphs of $y =  3 - x $ and $y = 9 - 2x$ .	[2]
	<b>(b)</b>	Solve the inequality $ 3 - x  > 9 - 2x$ .	[3]
			••••
	(c)	Use logarithms to solve the inequality $2^{3x-10} < 500$ . Give your answer in the form $x < a$ , where the value of $a$ is given correct to 3 significant figures.	ere [3]
			••••
	(d)	List the integers that satisfy both of the inequalities $ 3 - x  > 9 - 2x$ and $2^{3x-10} < 500$ .	[1]

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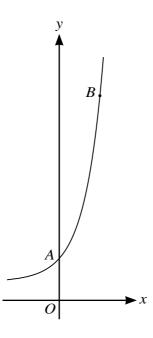
	<b>(b)</b>	Hence	find
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$\int_{2}^{7} \frac{6x^3 - 5x^2 - 24x - 4}{2x + 1}  \mathrm{d}x,$	
giving your answer in the form $a + \ln b$ , where $a$ and $b$ are integers.	[5]
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[5]

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6



The diagram shows the curve with parametric equations

$$x = 3 \ln(2t - 3),$$
  $y = 4t \ln t.$ 

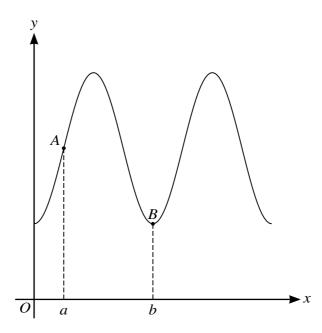
The curve crosses the y-axis at the point A. At the point B, the gradient of the curve is 12.

(a)	Find the exact gradient of the curve at A.	[5]

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	Use an iterative formula, based	on the	equat	ion in	<b>(b)</b> , to	find th	e value o	of $t$ at $B$	B, giving y	ou
	answer correct to 3 significant f									ac
	iteration to 5 significant figures.									[3
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7	(a)	Prove that $\sin 2x(\cot x + 3\tan x) \equiv 4 - 2\cos 2x$ .	[4]
			•••••
	<b>(b)</b>	Hence find the exact value of $\cot \frac{1}{12}\pi + 3 \tan \frac{1}{12}\pi$ .	[2]
			•••••

**(c)** 



The diagram shows the curve with equation  $y = 4 - 2\cos 2x$ , for  $0 < x < 2\pi$ . At the point A, the gradient of the curve is 4. The point B is a minimum point. The x-coordinates of A and B are a and b respectively.

Show that $\int_{a}^{b} (4 - 2\cos 2x) dx = 3\pi + 1.$	[5]
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## **Additional Page**

If you use the following lined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.

## 15

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