

Cambridge International AS & A Level

	CANDIDATE NAME			
	CENTRE NUMBER		CANDIDATE NUMBER	
	MATHEMATIC	S		9709/12
ວ	Paper 1 Pure Ma	athematics 1		February/March 2024
				1 hour 50 minutes
	You must answe	er on the question paper.		
*	You will need:	List of formulae (MF19)		

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

Find the exact value of $\int_3^\infty \frac{2}{x^2} dx$.	



3

The diagram shows part of the curve with equation $y = k \sin \frac{1}{2}x$, where k is a positive constant and x is measured in radians. The curve has a minimum point A.

(a) State the coordinates of A.

[1]

(b) A sequence of transformations is applied to the curve in the following order.

Translation of 2 units in the negative *y*-direction

Reflection in the *x*-axis

Find the equation of the new curve and determine the coordinates of the point on the new curve corresponding to A. [3]

Find the volue of a			
Find the value of <i>a</i> .			
	 	 •••••	
	 	 •••••	
	 	 •••••	

•	Drove that	$(\sin\theta + \cos\theta)$	•) •	$-2\tan\theta$	[2]	
)	1 love that	$\frac{(\sin\theta + \cos\theta)}{\cos^2\theta}$	9	$= 2 \tan \theta$.	[3]	
			(sin	$(\theta + \cos \theta)^2 = 1$		
)	Hence solv	ve the equati	on <u>(sin</u>	$\frac{\theta + \cos \theta)^2 - 1}{\cos^2 \theta} = 5 \tan^3 \theta \text{ for } -90^\circ < \theta$	9 < 90°. [3]	
))	Hence solv	ve the equati	on <u>(sin</u>	$\frac{\theta + \cos \theta)^2 - 1}{\cos^2 \theta} = 5 \tan^3 \theta \text{ for } -90^\circ < \theta$	9 < 90°. [3]	
))	Hence solv	ve the equati	on <u>(sin</u>	$\frac{\theta + \cos \theta)^2 - 1}{\cos^2 \theta} = 5 \tan^3 \theta \text{ for } -90^\circ < \theta$	9 < 90°. [3]	
))		ve the equati	on <u>(sin</u>		9 < 90°. [3]	
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5 A curve has the equation $y = \frac{3}{2x^2 - 5}$.

Find the equation of the normal to the curve at the point (2, 1), giving your answer in the form ax+by+c=0, where *a*, *b* and *c* are integers. [6]

is 432.
Find the value of the constant <i>a</i> . [5]

	Find the value of the constant <i>k</i> .	
(h)	Find the coordinates of <i>P</i> .	
(0)		
(0)		
(0)		
(0)		
(0)		

a)	An arithmetic progression is such that its first term is 6 and its tenth term is 19.5.	
	Find the sum of the first 100 terms of this arithmetic progression.	[4
	The sum to infinity of this geometric progression is denoted by S. The sum to infinity of even-numbered terms (i.e. $a_2, a_4, a_6,$) is denoted by S_E . Find the values of S and S.	
	even-numbered terms (i.e. $a_2, a_4, a_6,$) is denoted by S_E .	
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	even-numbered terms (i.e. $a_2, a_4, a_6,$) is denoted by S_E .	

	$f(x) = (3x-2)^2 + k$ and $g(x) = 5x - 1$,
whe	pre k is a constant.
(a)	Given that the range of the function gf is $gf(x) \ge 39$, find the value of <i>k</i> . [4]
(b)	For this value of k , determine the range of the function fg. [2]

The functions f and g are defined for all real values of x by

..... _____ (c) The function h is defined for all real values of x and is such that gh(x) = 35x + 19. Find an expression for $g^{-1}(x)$ and hence, or otherwise, find an expression for h(x). [3]



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The diagram shows the circle with centre C(-4, 5) and radius $\sqrt{20}$ units. The circle intersects the *y*-axis at the points *A* and *B*. The size of angle *ACB* is θ radians.

That the equation	of the tangent to the circle at the point $(-6, 9)$.	
Find the equation	of the circle in the form $x^2 + y^2 + ax + by + c = 0$.	
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Find the equation	of the circle in the form $x^2 + y^2 + ax + by + c = 0$.	

(c)	Find the value of θ correct to 4 significant figures.	[3]
(d)	Find the perimeter and area of the segment shaded in the diagram.	[4]



The diagram shows the curve with equation $y = 2x^{-\frac{2}{3}} - 3x^{-\frac{1}{3}} + 1$ for x > 0. The curve crosses the *x*-axis at points *A* and *B* and has a minimum point *M*.

.....

(a) Find the exact coordinates of M.

. . .

11

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[4]

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Additional page

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