

Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

856701363

MATHEMATICS 9709/32

Paper 3 Pure Mathematics 3

May/June 2024

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has 20 pages. Any blank pages are indicated.

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[1]

(a) Sketch the graph of y = |x - 2a|, where a is a positive constant.

1

(b)	Solve the inequality $2x - 3a < x - 2a $.	

Express $\frac{6x^2 - 9x - 16}{2x^2 - 5x - 12}$ in partial fractions.	
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	••••••

a)	Show that the graph of y against x is a straight line.	[3]
		• • • • • • • • • • • • • • • • • • • •
h)	Given that $a = b^3$ state the equation of the straight line in the form $v = nx + a$ where n	and a are
(b)	Given that $a = b^3$, state the equation of the straight line in the form $y = px + q$, where p rational numbers in their simplest form.	[2]
(b)	rational numbers in their simplest form.	[2]
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Find the	gradient of	f the curve	at the po	int wher	e $y = 1$	•				[6
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5	(a)	It is given that the equation $e^{2x} = 5 + \cos 3x$ has only one root.	
		Show by calculation that this root lies in the interval $0.7 < x < 0.8$.	[2]
			•••••
			•••••
	(b)	Show that if a sequence of values in the interval $0.7 < x < 0.8$ given by the iterative formula	
		$x_{n+1} = \frac{1}{2} \ln \left(5 + \cos 3x_n \right)$	
		converges then it converges to the root of the equation in part (a).	[1]
			•••••
			•••••
	(c)	Use this iterative formula to determine the root correct to 3 decimal places. Give the result of eiteration to 5 decimal places.	each [3]

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The diagram shows the curve $y = xe^{-ax}$, where a is a positive constant, and its maximum point M.

Find the exact coordinates of M .	

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	exact value of \int	$-\frac{1}{8}\pi$			
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(a)	Find a vector equation for l_1 .	[3
Γhe	line l_2 has equation $\mathbf{r} = -2\mathbf{i} + \mathbf{j} + 4\mathbf{k} + \mu(3\mathbf{i} + \mathbf{j} - 2\mathbf{k})$.	
(b)	Find the coordinates of the point of intersection of l_1 and l_2 .	[4

Find the position ve	ctor of D .			
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(a)	Express $z\omega$ in the form $a+bi$, where a and b are real and in exact surd form.	[1
(b)	Express z and ω in the form $re^{i\theta}$, where $r > 0$ and $-\pi < \theta \le \pi$. Give the exact values in each case.	of r and ϵ
		•••••
		•••••
(c)	On an Argand diagram, the points representing ω and $z\omega$ are A and B respectively.	
	Prove that <i>OAB</i> is an isosceles right-angled triangle, where <i>O</i> is the origin.	

(d)	Using your answers to part (b) , prove that $\tan \frac{5}{12}\pi$	$=\frac{\sqrt{3}+1}{\sqrt{3}-1}.$	[3]

10	(a)	By writing $y = \sec^3 \theta$ as $\frac{1}{\cos^3 \theta}$, show that $\frac{dy}{d\theta} = 3\sin\theta \sec^4 \theta$. [2]	
	(b)	The variables x and 0 satisfy the differential equation	
	(D)	The variables x and θ satisfy the differential equation $\left(x^2 + 9\right)\sin\theta \frac{d\theta}{dx} = (x+3)\cos^4\theta.$	
		It is given that $x = 3$ when $\theta = \frac{1}{3}\pi$.	
		Solve the differential equation to find the value of $\cos \theta$ when $x = 0$. Give your answer correct to 3 significant figures.	

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Additional page

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