



Cambridge International AS & A Level

CANDIDATE NAME			
CENTRE NUMBER	CANDIDATE NUMBER		

MATHEMATICS 9709/12

Paper 1 Pure Mathematics 1

October/November 2024

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

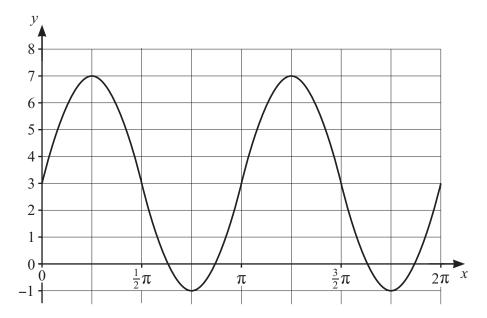
INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has 20 pages. Any blank pages are indicated.



The diagram shows the curve with equation $y = a\sin(bx) + c$ for $0 \le x \le 2\pi$, where a, b and c are positive constants.

State the values of a , b and c .	[3]

(b) For these values of a, b and c, determine the number of solutions in the interval $0 \le x \le 2\pi$ for each of the following equations:

(i)
$$a\sin(bx) + c = 7 - x$$
 [1]

(ii)
$$a\sin(bx) + c = 2\pi(x-1)$$
. [1]

(a)

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The first term of an arithmetic progression is -20 and the common difference is 5.

(a)	Find the sum of the first 20 terms of the progression.	[2]
It is	given that the sum of the first $2k$ terms is 10 times the sum of the first k terms.	
	Find the value of k .	[3]
(~)		

(a)	Find and simplify an expression for the gradient of the chord AB in terms of h .	[3]
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(b)	Explain how the gradient of the curve at the point A can be deduced from the answer to part (and state the value of this gradient.	(a) , [2]
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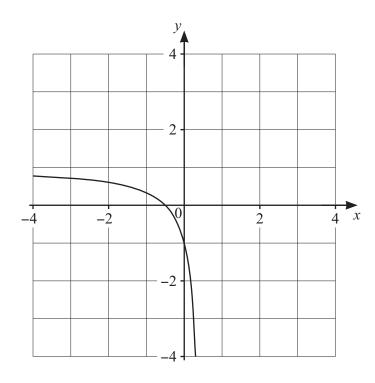
Find the term independent of x in the expansion of each of the following:

(a)	$\left(x + \frac{3}{x^2}\right)^6$	[2]
(b)	$(4x^3 - 5)\left(x + \frac{3}{x^2}\right)^6$.	[4]

State the value of f(-1).

(ii)

(a) (i)



The diagram shows the graph of y = f(x). Sketch the graph of $y = f^{-1}(x)$ on this diagram. Show any relevant mirror line. [2]

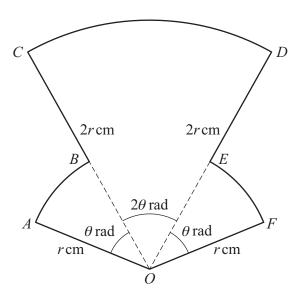
Find an expression for $f^{-1}(x)$ and state the domain of the function f^{-1} . (iii) [4]

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The	function α is defined by $\alpha(x) = 2x + 2$ for $x \in \mathbb{D}$	
	e function g is defined by $g(x) = 3x + 2$ for $x \in \mathbb{R}$.	
	e function g is defined by $g(x) = 3x + 2$ for $x \in \mathbb{R}$. Solve the equation $f(x) = gf(\frac{1}{4})$.	[3]
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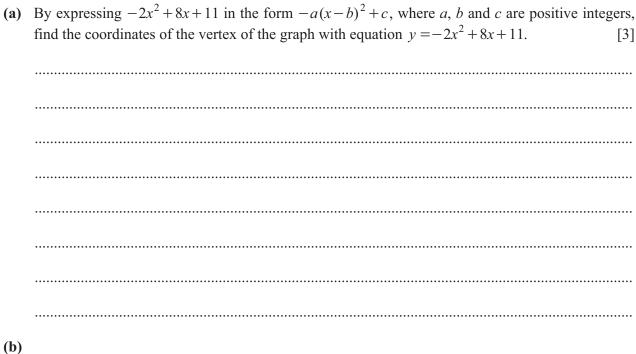
The diagram shows a metal plate OABCDEF consisting of sectors of two circles, each with centre O. The radii of sectors AOB and EOF are r cm and the radius of sector COD is 2r cm. Angle AOB = angle EOF = θ radians and angle COD = 2θ radians.

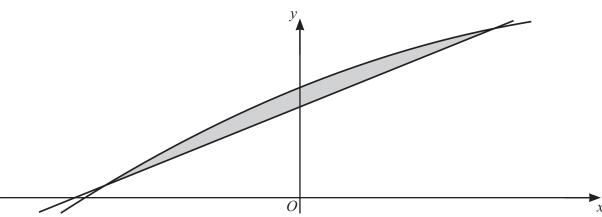
It is given that the perimeter of the plate is 14 cm and the area of the plate is 10 cm².

Given that $r > \frac{3}{2}$ and $\theta < \frac{3}{4}$, find the values of r and θ .			
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The diagram shows part of the curve with equation $y = -2x^2 + 8x + 11$ and the line with equation y = 8x + 9.

Find the area of the shaded region.				

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- 8 The equation of a circle is $x^2 + y^2 + px + 2y + q = 0$, where p and q are constants.
 - (a) Express the equation in the form $(x-a)^2 + (y-b)^2 = r^2$, where a is to be given in terms of p and r^2 is to be given in terms of p and q. [2]

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The line with equation x + 2y = 10 is the tangent to the circle at the point A(4, 3).

(b) (i) Find the equation of the normal to the circle at the point A. [3]



	 	
`	Find the values of n and a	

Find the values of p and q .	[5]
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- The equation of a curve is $y = \frac{1}{2}k^2x^2 2kx + 2$ and the equation of a line is y = kx + p, where k and p are constants with 0 < k < 1.
 - (a) It is given that one of the points of intersection of the curve and the line has coordinates $\left(\frac{5}{2}, \frac{1}{2}\right)$.

Find the values of k and p , and find the coordinates of the other point of intersection.	[7]
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(b)	It is given instead that the line and the curve do not intersect.
	Find the set of possible values of p . [3]

equ	function f with domain $x > 0$ is such that $f'(x) = 8(2x-3)^{\frac{1}{3}} - 10x^{\frac{2}{3}}$. It is given that the curve with ation $y = f(x)$ passes through the point $(1, 0)$.
(a)	Find the equation of the normal to the curve at the point $(1, 0)$. [3]
(b)	Find $f(x)$. [4]

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It is given that the equation f'(x) = 0 can be expressed in the form

 $125x^2 - 128x + 192 = 0.$

Determine, making your reasoning clear, whether f is an increasing function, a decreasing function or neither.

Additional page

If you use the following page to complete the answer to any question, the question number must be clearly shown.		



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