

Cambridge International AS & A Level

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
MATHEMATI	cs		9709/12
Paper 1 Pure N	Mathematics 1		February/March 2022
			1 hour 50 minutes
You must answ	ver on the question paper.		

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has 20 pages. Any blank pages are indicated.

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Find $f(x)$).						
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A curve has equation $y = x^2 + 2cx + 4$ and a straight line has equation $y = 4x + c$, where c is a constant.
Find the set of values of c for which the curve and line intersect at two distinct points. [5]

3 Find the term independent of *x* in each of the following expansions.

(a) $\left(3x + \frac{2}{x^2}\right)^6$ [3] **(b)** $\left(3x + \frac{2}{x^2}\right)^6 (1 - x^3)$ [3]

4 The first term of a geometric progression and the first term of an arithmetic progression are both equal to *a*.

The third term of the geometric progression is equal to the second term of the arithmetic progression.

The fifth term of the geometric progression is equal to the sixth term of the arithmetic progression.

Given that the terms are all positive and not all equal, find the sum of the first twenty terms of the arithmetic progression in terms of a. [6]

..... The functions f and g are defined by $f(x) = x^2$ for $x \in \mathbb{R}$, $g(x) = 2x^2 - 8x + 14$ for $x \in \mathbb{R}$. (b) Describe fully a sequence of transformations that maps the graph of y = f(x) onto the graph of y = g(x), making clear the order in which the transformations are applied. [4]

(a) Express $2x^2 - 8x + 14$ in the form $2[(x-a)^2 + b]$.

5

[2]



The circle with equation $(x + 1)^2 + (y - 2)^2 = 85$ and the straight line with equation y = 3x - 20 are shown in the diagram. The line intersects the circle at *A* and *B*, and the centre of the circle is at *C*.

(a)	Find, by calculation, the coordinates of A and B.	[4]
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(b) Find an equation of the circle which has its centre at C and for which the line with equation y = 3x - 20 is a tangent to the circle. [4]

-	(-)	C1	$\sin\theta + 2\cos\theta$	$\sin\theta - 2\cos\theta$	4	٢ ٨ ٦
7	(a)	Show that	$\cos\theta - 2\sin\theta$	$-\frac{\sin\theta - 2\cos\theta}{\cos\theta + 2\sin\theta} =$	$\overline{5\cos^2\theta-4}$.	[4]
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Hence solve the equation	5111 0 + 2 0 0 5 0	$-\frac{1}{2} = 5$ for $0^\circ \le \theta \le 180^\circ$
inenee sorre me equation	$\cos\theta - 2\sin\theta$	$\cos\theta + 2\sin\theta$
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		Hence solve the equation $\frac{\sin \theta + 2\cos \theta}{\cos \theta - 2\sin \theta}$



12

The diagram shows the circle with equation $(x - 2)^2 + y^2 = 8$. The chord *AB* of the circle intersects the positive *y*-axis at *A* and is parallel to the *x*-axis.

[3]

(a) Find, by calculation, the coordinates of *A* and *B*.

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(b) Find the volume of revolution when the shaded segment, bounded by the circle and the chord AB, is rotated through 360° about the x-axis. [5]

9 Functions f, g and h are defined as follows:

f: $x \mapsto x - 4x^{\frac{1}{2}} + 1$ for $x \ge 0$, g: $x \mapsto mx^2 + n$ for $x \ge -2$, where *m* and *n* are constants, h: $x \mapsto x^{\frac{1}{2}} - 2$ for $x \ge 0$.

(a) Solve the equation f(x) = 0, giving your solutions in the form $x = a + b\sqrt{c}$, where *a*, *b* and *c* are integers. [4]

)	Given that $f(x) \equiv gh(x)$, find the values of <i>m</i> and <i>n</i> .	[4]
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16

The diagram shows a circle with centre A of radius 5 cm and a circle with centre B of radius 8 cm. The circles touch at the point C so that ACB is a straight line. The tangent at the point D on the smaller circle intersects the larger circle at E and passes through B.

[5]

(a) Find the perimeter of the shaded region.

.....

17

(b)	Find the area of the shaded region. [3]

,	Find, in terms of k , the values of x at which there is a stationary point.	
		•••••

The function f has a stationary value at x = a and is defined by

$$f(x) = 4(3x - 4)^{-1} + 3x$$
 for $x \ge \frac{3}{2}$.

(b) Find the value of *a* and determine the nature of the stationary value. [3] (c) The function g is defined by $g(x) = -(3x+1)^{-1} + 3x$ for $x \ge 0$. Determine, making your reasoning clear, whether g is an increasing function, a decreasing function or neither. [2]

Additional Page

If you use the following lined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.

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