



## **Cambridge International Examinations**

Cambridge International Advanced Subsidiary and Advanced Level

CANDIDATE NAME								
CENTRE NUMBER			ANDIDATE JMBER					
MATHEMATICS							9709/	12
Paper 1 Pure Ma	ıthema	itics 1 (P	1)		0	ctober/No	ovember 20	18
						1 ho	ur 45 minut	es
Candidates answ	er on t	he Quest	ion Pape	∍r.				
Additional Materia	als:	List of F	ormulae	∍ (MF9)				

## **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer **all** the questions in the space provided. If additional space is required, you should use the lined page at the end of this booklet. The question number(s) must be clearly shown.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

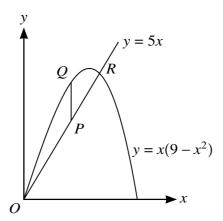
The total number of marks for this paper is 75.



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2	Showing all necessary working, find $\int_{1}^{4} \left( \sqrt{x} + \frac{2}{\sqrt{x}} \right) dx$ .	[4]
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3



The diagram shows part of the curve  $y = x(9 - x^2)$  and the line y = 5x, intersecting at the origin O and the point P. Point P lies on the line y = 5x between O and P and the P-coordinate of P is P-coordinate of P is P-coordinate of P-c

(i)	Express the length of $PQ$ in terms of $t$ , simplifying your answer.	[2]
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<b>(**</b> \		
(11)	Given that $t$ can vary, find the maximum value of the length of $PQ$ .	[3]
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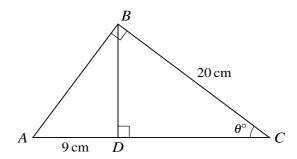
4 Functions f and g are defined by
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$$f: x \mapsto 2 - 3\cos x$$
 for  $0 \le x \le 2\pi$ ,  
 $g: x \mapsto \frac{1}{2}x$  for  $0 \le x \le 2\pi$ .

(i)	Solve the equation $fg(x) = 1$ .	[3]
(ii)	Sketch the graph of $y = f(x)$ .	[3]

		are positive.
(i)	Find the value of $x$ and the value of $y$ .	

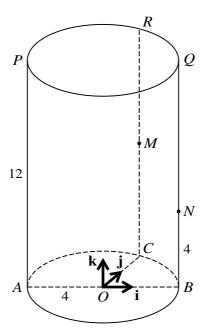
Find the fourth term of each progression.	[3]



The diagram shows a triangle ABC in which BC = 20 cm and angle  $ABC = 90^{\circ}$ . The perpendicular from B to AC meets AC at D and AD = 9 cm. Angle  $BCA = \theta^{\circ}$ .

(i)	By expressing the length of <i>BD</i> in terms of $\theta$ in each of the triangles <i>ABD</i> and <i>DBC</i> , show that $20 \sin^2 \theta = 9 \cos \theta$ . [4]

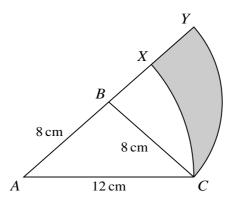
Hence, showing all necessary working, calculate $\theta$ .	
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The diagram shows a solid cylinder standing on a horizontal circular base with centre O and radius 4 units. Points A, B and C lie on the circumference of the base such that AB is a diameter and angle  $BOC = 90^{\circ}$ . Points P, Q and R lie on the upper surface of the cylinder vertically above A, B and C respectively. The height of the cylinder is 12 units. The mid-point of CR is M and N lies on BQ with BN = 4 units.

Unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are parallel to OB and OC respectively and the unit vector  $\mathbf{k}$  is vertically upwards.

Evaluate $\overrightarrow{PN} \cdot \overrightarrow{PM}$ and hence find angle $MPN$ .	[7]
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The diagram shows an isosceles triangle ACB in which AB = BC = 8 cm and AC = 12 cm. The arc XC is part of a circle with centre A and radius 12 cm, and the arc YC is part of a circle with centre B and radius 8 cm. The points A, B, X and Y lie on a straight line.

(i)	Show that angle $CBY = 1.445$ radians, correct to 4 significant figures.	[3]
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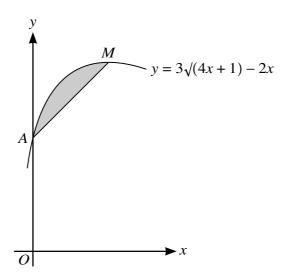

)	Express $2x^2 - 12x + 7$ in the form $2(x + a)^2 + b$ , where a and b are constants.	[2
		•••••
		•••••
) ;	State the range of f.	

The	ne function g is defined by $g: x \mapsto 2x^2 - 12x + 7$ for $x \le k$ .		
(iii)	State the largest value of $k$ for which g has an inverse.	[1]	
(iv)	Given that g has an inverse, find an expression for $g^{-1}(x)$ .	[3]	

	e set of val	lues of $k$ f	for which	the line doe	s not meet	the curve.		
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(iii)	Find the equation of the perpendicular bisector of the line joining $A$ and $B$ .	[3]

11



The diagram shows part of the curve  $y = 3\sqrt{(4x+1)} - 2x$ . The curve crosses the y-axis at A and the stationary point on the curve is M.

(i)	Obtain expressions for $\frac{dy}{dx}$ and	$\int y\mathrm{d}x.$	[5]

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## **Additional Page**

If you use the following fined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.

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