

Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

MATHEMATICS 9709/12

Paper 1 Pure Mathematics 1

October/November 2021

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has 20 pages.

Solve the equation $2\cos\theta = 7$ -	$\cos \frac{\overline{\theta}}{\theta}$ for -50° $< 0^{\circ}$ $> 0^{\circ}$.	[4]

	Describe fully the two single transformations that have been combined to give the resultransformation.	lting [3
ie		
	point $P(5, 6)$ lies on the transformed curve $y = f(2x) - 3$. State the coordinates of the corresponding point on the original curve $y = f(x)$.	[2
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3	The function	T 10	пеппеп	as tollows:

$$f(x) = \frac{x+3}{x-1} \text{ for } x > 1.$$

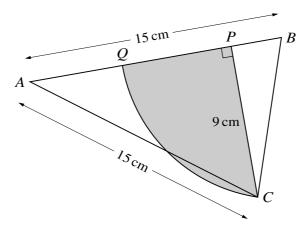
(a)	Find the value of $ff(5)$.	[2]
(b)	Find an expression for $f^{-1}(x)$.	[3]
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Find the equation of the curve					
Find the equation of the curve.					
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Find the exact value of x .	[3]
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Hence find the exact sum of the first 25 terms of the progression.	[3]
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Hence find the exact sum of the first 25 terms of the progression.	[3

F	ind the tenth term, giving your answer in exact form.	
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In the diagram the lengths of AB and AC are both 15 cm. The point P is the foot of the perpendicular from C to AB. The length CP = 9 cm. An arc of a circle with centre B passes through C and meets AB at Q.

Show that angle $ABC = 1.25$ radians, correct to 3 significant figures.	[2]

Pζ	^{2}Q .	
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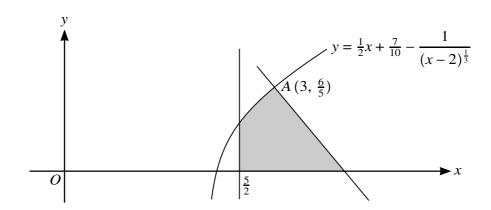
3 (a	1) It is given that in the expansion of $(4 + 2x)(2 - ax)^5$, the coefficient of x^2 is	-15.
	Find the possible values of a .	[4]

given that there is only one value of a which leads to this value of k .	
Find the values of k and a .	
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)	Find the rate at which the radius of the mound is increasing at the instant when the radius is

10	The	function f is defined by $f(x) = x^2 + \frac{k}{x} + 2$ for $x > 0$.
	(a)	Given that the curve with equation $y = f(x)$ has a stationary point when $x = 2$, find k . [3]

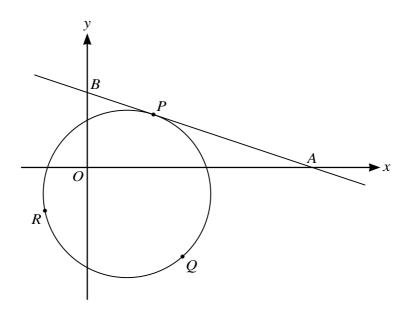
Determine the nature of the stationary point.	
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Given that this is the only stationary point of the curve, find the range of f.	



The diagram shows the line $x = \frac{5}{2}$, part of the curve $y = \frac{1}{2}x + \frac{7}{10} - \frac{1}{(x-2)^{\frac{1}{3}}}$ and the normal to the curve at the point $A\left(3, \frac{6}{5}\right)$.

Find the x-coordinate of the point where the normal to the curve meets the x -axis.	[5]
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Find the area of the shaded region, giving your answer correct to 2 decimal places.	
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The diagram shows the circle with equation $x^2 + y^2 - 6x + 4y - 27 = 0$ and the tangent to the circle at the point P(5, 4).

(a) The tangent to the circle at P meets the x-axis at A and the y-axis at B.

Find the area of triangle OAB , where O is the origin.	[5]
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J	Points Q and R also lie on the circle, such that PQR is an equilateral triangle.
]	Find the exact area of triangle PQR . [3]
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Additional Page

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