

## Cambridge IGCSE™

# CAMBRIDGE INTERNATIONAL MATHEMATICS Paper 6 (Extended) MARK SCHEME Maximum Mark: 60 Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the March 2021 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

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## **Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

### GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

## GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

### GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

### GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

## GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Ma	Maths-Specific Marking Principles				
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.				
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.				
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.				
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).				
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.				
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.				

### MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

## Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

## **Abbreviations**

awrt answers which round to
cao correct answer only
dep dependent

ET follow through after error

FT follow through after error isw ignore subsequent working nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

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Question	Answer	Marks	Partial Marks
A	INVESTIGATION ENCLOSED CUBOIDS		
1(a)	26	1	
1(b)(i)	5	1	
1(b)(ii)	$5^{3}-1$ oe or $4 \text{ [layers]} \times 25 + \text{ [1 layer]} 24$ oe or $their 26 + 6 \text{ [faces]} \times 3^{2} + 12 \text{ [edges]} \times 3 + 8 \text{ [vertices]} \text{ oe}$ or $their 26 + 5^{3} - 3^{3}$ oe	C1	
	124	1	
1(c)	Total number of cubes = number of white cubes + 1 oe	1	
1(d)	$7^3 - 1$ oe or at least three differences of 2	C1	
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4	<b>B1</b> for 7 and 9 <b>B1</b> for 342 <b>B1</b> for $2n + 1$ oe <b>B1FT</b> for $(their (2n + 1))^3 - 1$ oe
2(a)	4 <sup>3</sup> is the [total] volume of the cube [in cm <sup>3</sup> ] 2 <sup>3</sup> is the volume of the grey cube [in cm <sup>3</sup> ] [The difference is the number of white cubes oe]  OR 4 [cm] is the outer cube edge length oe 2 [cm] is the grey cube edge length oe	2	B1 for each  OR  B1 for two correct statements
	Cubing edge length gives volume oe [The difference is the number of white cubes oe]		
2(b)	$6^3 - 2^3$ oe or $8^3 - 2^3$ oe	C1	
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3	<b>B1</b> for $2^{nd}$ row correct <b>B1</b> for 208 and 504 <b>B1FT</b> for $(their (2n + 2))^3 - 2^3$ oe
3(a)		2	B1 for row 2 correct B1FT for $(their (2n + 3))^3 - 3^3$ oe

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Question		Answer	Marks	Partial Marks
3(b)	Edge length of grey cube	W	2	<b>B1</b> for $(2n+e)^3$ oe or for $-e^3$
	1	$(2n+1)^3-1$		
	2	$(2n+2)^3-2^3$		
	3	$(2n+3)^3-3^3$		
	е	$(2n+e)^3-e^3  \text{oe}$		
4(a)	$4 \times 5 \times 7 - 2 \times 3 \times 5$		C2	C1 for $4 \times 5 \times 7$ or 4, 5 and 7 are edge lengths soi
	or			or
	$2(5\times3+5\times2$	$(2 + 3 \times 2)[faces] + 4(5 + 3 + 2)[edges] + 8[corners]$	]	for $2(5 \times 3 + 5 \times 2 + 3 \times 2) + 4(5 + 3 + 2)$
	110		1	
4(b)	W = (a+2n)(a+2n)(a+2n)	(b+2n)(c+2n) - abc isw	2	B1 for $a + 2n$ or $b + 2n$ or $c + 2n$ or for $(a + 2)(b + 2)(c + 2) - abc$ or for using any stated numerical $n$

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Question	Answer	Marks	Partial Marks
5	2k + 16 and $k + 16$ seen	C1	
	(2k+16)(k+16) = 546	C1	FT their length for $(2k + a)$ and $(k + a)$
	Method 1 Sketch of quadratic with exactly one positive intersection with horizontal line for 546 or 273.	C2	
	OR  Method 2  Correct expansion of <i>their</i> equation if of the form $(ak + b)(ck + d) = 546$ .	C1	
	Method of solving <i>their</i> quadratic equation with non-zero term in <i>k</i>	C1FT	Dependent on first C1. Sketch of quadratic with exactly one positive intersection with horizontal axis or horizontal line. or factorisation or substitution into the quadratic formula
	5	1	

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Question	Answer	Marks	Partial Marks
В	MODELLING ENCLOSURES FOR CATS		
6(a)(i)	$\frac{1}{3}\pi \left(\frac{d}{2}\right)^2 h \text{ or } \frac{1}{3}\pi \frac{d^2}{4}h$	1	
6(a)(ii)	$[V=] \frac{\pi d^3}{12} \text{ isw}$	2	<b>B1</b> for a correct unsimplified form e.g. $\frac{1}{2} \times \frac{4}{3} \pi \left(\frac{d}{2}\right)^3$ oe
6(b)	[h=]d	1	FT their (a)(ii)
6(c)(i)	$[V=] \frac{\pi d^2}{12} [\times] \frac{d}{2} \text{ oe}$	C1	
	$[V=] \frac{\pi d^3}{24}$	1	
6(c)(ii)	Cone with valid justification e.g. denominator for cone is greater or $\frac{1}{12}$ or $\frac{2}{24} > \frac{1}{24}$ oe or $0.8\dot{3} > 0.042$ (or $0.041\dot{6}$ ) or ratio = 1:2 oe	1	FT their $\frac{1}{12}$ in part (a)(ii) > their $\frac{1}{24}$ in part (c)(i) only if numerators for volume the same.
7(a)	0.5 + 2.8 + 1 [= 4.3] oe and [4.3] × 2 [= 8.6] oe	1	
7(b)	$r = \sqrt{\frac{8.6}{\pi}} \text{ oe}$ or $d^2 = \frac{8.6 \times 4}{\pi}$ or better	C1	
	3.31	1	If C0 and 0 scored, SC1 for 2.34
7(c)	Height 1.65 is less than 2[m] or 1.65 less than highest point oe	1	FT $\frac{1}{2}$ their 3.31 if less than 2.
8(a)	$\frac{\pi d^2 h}{12} = 10  \text{oe}$	C1	
	$h = \frac{120}{\pi d^2}$	1	

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Question	Answer	Marks	Partial Marks
8(b)	Correct sketch	2	<ul> <li>B1 for correct shape, not cutting the d-axis but &lt; 0.6 at d = 12</li> <li>B1 for correct shape to the right of d = 1.2</li> </ul>
8(c)	$\frac{1}{3}\pi r^2 \times 2 = 10$ OR	C2	$C1 \frac{1}{3}\pi r^2 \times 2$
	$\pi d^2 = 60$ oe or $\pi (2r)^2 = 60$ and $\pi \times \frac{d^2}{4}$ or $4 \pi r^2 = 60$		C1 for each
	OR $[d=]\sqrt{\frac{120}{2\pi}} \text{ oe or } r = \sqrt{\frac{15}{\pi}} \text{ oe}$ and $\pi \times \left(\frac{\sqrt{\frac{120}{2\pi}}}{2}\right)^2$ or better OR		C1 for each
	[d=] 4.37[0] or $r = 2.185$ or 2.19 and $\pi \times \left(\frac{their \ 4.37}{2}\right)^2$ oe or $\pi \times (their \ 2.185)^2$		C1 for each
	15	1	
9(a)	4	1	
9(b)	Using $\frac{\pi r^2 h}{2}$ with correct substitution of $\frac{d}{2}$ and $w$ leading to $\frac{\pi d^2 w}{8}$	2	B1 for using $\frac{\pi r^2 h}{2}$ or correct substitution of $\frac{d}{2}$ and $w$ into cylinder formula
9(c)(i)	$\frac{\pi d^2 w}{8} = 10 \text{ and } \pi d^2 w = 80 \text{ leading to } w = \frac{80}{\pi d^2}$	1	

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Question	Answer	Marks	Partial Marks
9(c)(ii)	Correct sketch	1	Correct shape that does not cross either axis
9(d)(i)	$w = \frac{8.6}{d}$	1	
9(d)(ii)	Correct sketch	2	B1 for correct shape, not touching either axis B1 dep for one point of intersection,  If 0 scored, SC1 for one point of intersection and a curve with only one axis as an asymptote.
9(e)	Intersection marked on graph, or use of intersection point stated. or $\frac{80}{\pi d^2} = their \frac{8.6}{d}$ or better	C1	
	$[d=] 2.96[] \text{ or } \frac{80}{8.6\pi} \text{ oe}$	1	
	1.48[]	1	FT their (d)
10	Choice with valid reason e.g. Cone because half-cylinder is not high enough. Half-cylinder has space that is easier to use.	1	FT their 9(e)

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