

### **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

#### **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/41

Paper 4 (Extended) May/June 2017

MARK SCHEME
Maximum Mark: 120

D		h	ı	_	h	ed	ı
г	u	IJ	ш	5	п	eu	ı

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2017 series for most Cambridge IGCSE<sup>®</sup>, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

 ${\rm \rlap{R}\hskip-1pt B}$  IGCSE is a registered trademark.



### MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

### Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

#### **Abbreviations**

awrt answers which round to cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

© UCLES 2017 Page 2 of 7

Question	Answer	Marks	Partial Marks
1(a)(i)	24 4 <i>n</i> final answer	2	B1 for each
1(a)(ii)	-11 -2n + 1 oe final answer	3	<b>B1</b> for $-11$ <b>M1</b> for $kn + 1$ (where $k < 0$ ) or $-2n + k$
1(a)(iii)	$3n^2$ oe final answer	3	<b>B1</b> for 108 <b>M1</b> for $kn^2$ [+ q]
1(a)(iv)	$216$ $n^3$ oe final answer	2	B1 for each
1(b)	$337$ $n^3 + 3n^2 + 2n + 1$ oe final answer	3	<b>B1</b> for 337 <b>M1</b> for adding <i>their n</i> th terms or 3rd differences = 6 and a cubic with numerical coefficients for the answer
2(a)	31.1	2	M1 for evidence of at least 3 correct midpoints
2(b)(i)	[7], 20, 40, 72, 100	1	
2(b)(ii)	Correct Graph	3	B1 for plotting <i>their</i> points at upper group limit (but points must be increasing vertically) B1 for 4 or 5 correct FT vertical plots (must be increasing)
2(c)(i)	32.5 to 34.5	1	FT their graph, dependent on increasing curve
2(c)(ii)	16.5 to 20	2	FT their graph, dependent on increasing curve
			<b>B1</b> for UQ = 40.5 to 42 or LQ = 22 to 24 or <b>M1</b> for <i>their</i> UQ – <i>their</i> LQ
2(c)(iii)	3 to 4	3	FT their graph, dependent on increasing curve
			M2 for <i>their</i> 55 th percentile (34 to 36) and <i>their</i> 45 th percentile (31 to 33) or M1 for <i>their</i> 45th percentile (31 to 33) or <i>their</i> 55th percentile (34 to 36) or SC3 for e.g. 32 to 35
3(a)	49.8 or 49.84 to 49.85	3	M2 for $\frac{30}{\sin 37}$ oe or M1 for $\sin 37 = \frac{30}{AC}$ oe
3(b)	39.7 or 39.8 or 39.74 to 39.81	3	M2 for $\frac{30}{\tan 37}$ or their (a) × cos 37 oe or M1 for tan 37 = $\frac{30}{BC}$ or cos 37 = $\frac{BC}{their(a)}$ oe

© UCLES 2017 Page 3 of 7

Question	Answer	Marks	Partial Marks
3(c)	21.7 or 21.8 or 21.67 to 21.81	3	M2 for $\frac{30}{\tan 26} - their(b)$ or $\frac{(their(a)) \times \sin(180 - (180 - 37) - 26)}{\sin 26}$ oe or M1 for $\frac{30}{\tan 26}$ or $\frac{their(a)}{\sin 26} = \frac{CD}{\sin(180 - (180 - 37) - 26)}$ oe
3(d)	325 or 326 or 327 or 325[.0] to 327.2	2	M1 for $\frac{1}{2} \times their(c) \times 30$ oe
4(a)	Correct triangle (2, 1) (3, 1) (2, 4)	2	<b>B1</b> for translation $\begin{pmatrix} k \\ -4 \end{pmatrix}$ or $\begin{pmatrix} 0 \\ k \end{pmatrix}$
4(b)	Correct triangle (-5, 2) (-5, 3) (-8, 2)	2	<b>B1</b> for correct rotation, incorrect centre or for rotation 90° clockwise, correct centre
4(c)	Rotation [Centre] (0, 0) 90° clockwise oe	2	B1 for each
4(d)	Correct triangle (-5, -2) (-5, -3) (-8, -2)	3	<b>B1</b> for $y = -x$ soi <b>M1</b> for correct shape, incorrect location
4(e)	Reflection <i>x</i> -axis oe	2	B1 for each
5(a)	[Angle between] tangent [and] radius / diameter [=90] oe	1	
5(b)(i)	134	2	<b>M1</b> for 360 – 90 – 90 – 46 oe
5(b)(ii)	23	2	<b>M1</b> for (180 – <i>their</i> (i)) ÷ 2 oe
5(b)(iii)	67	2	FT (their (i)) ÷ 2 M1 for (their (i)) ÷ 2 oe
5(b)(iv)	113	2	FT 180 – their (iii) or (360 – their (i)) ÷ 2 M1 for 180 – their (iii) or (360 – their (i)) ÷ 2 oe
5(c)	44	3	<b>M2</b> for $180 - 67 - 23 - 23 - 23$ oe or $360 - 226 - 67 - 23$ oe or <b>B1</b> for angle $OBC = 23$ or $226$ seen

© UCLES 2017 Page 4 of 7

Question	Answer	Marks	Partial Marks
6(a)	8	3	M1 for $y = \frac{k}{x^2}$ oe A1 for $k = 128$ OR
			M2 for $32 \div \left(\frac{4}{2}\right)^2$ oe or M1 for $\frac{y}{32} = \frac{\frac{1}{4^2}}{\frac{1}{2^2}}$ oe
6(b)	$[\pm]$ $\frac{1}{2}$ oe	2	M1 for $x^2 = \frac{their \ k}{512}$ oe or $2 \times \sqrt{\frac{32}{512}}$ oe
6(c)	$[x = \pm] \sqrt{\frac{128}{y}}$ oe final answer	3	M1 for multiplication by $x^2$ M1 for division by $y$ or for square root
7(a)	Correct Graph  10 y  (x)=abx(9-x-2)  x 4	4	B1 for maximum point on or close to y-axis B1 for correct shape between their –3 and 3 B1 for mod graph
7(b)	$[x = ] \pm 4, \pm \sqrt{2}$ or $\pm 1.41$ or $\pm 1.414$	2	<b>B1</b> for any 2 correct answers
7(c)	k > 9 k = 0	2	B1 for each
8(a)	Correct values inside circles  M 7 4 6 8 12 [4] 9 T	3	B2 for 4 or 5 regions correct B1 for 2 or 3 regions correct
8(b)(i)	17	1	FT their diagram
8(b)(ii)	11	1	FT their diagram

© UCLES 2017 Page 5 of 7

Question	Answer	Marks	Partial Marks
8(c)	$\frac{4}{56}$ oe	2	FT their 4 M1 for $\frac{their 4}{k}$ ( $k > their 4$ ) or $\frac{p}{56}$ ( $p < 56$ )
8(d)	$\frac{1190}{3080}$ oe	2	<b>M1</b> for $\frac{35}{56} \times \frac{34}{55}$
8(e)	$\frac{6}{25}$ oe	2	FT their 6 M1 for $\frac{their 6}{k}$ $(k > their 6)$ or $\frac{p}{25}$ $(p < 25)$
8(f)	$\frac{12}{870}$ oe	3	M2 for $\frac{their 4}{30} \times \frac{(their 4) - 1}{29}$ (their 4 < 30) or M1 for $\frac{a}{30} \times \frac{a - 1}{29}$ (their a < 30)
9(a)	$[\cos x =] \frac{8^2 + 6^2 - 2^2}{2 \times 6 \times 8}$ oe	M2	<b>M1</b> for $12^2 = 8^2 + 6^2 - 2 \times 8 \times 6 \cos[]$
	117.3 or 117.2 to 117.3	B1	
9(b)	$[\sin =] \frac{6 \times \sin(their(a))}{12} \text{ oe}$	M2	M1 for $\frac{6}{\sin A} = \frac{12}{\sin(their(a))}$ oe
	26.4 or 26.5 or 26.37 to 26.46	B1	
10(a)	Correct Graph    S(x)=2sin(x)+cos(x)	3	M1 for sine graph with one max and one min A1 for x-intercepts at 150 and 330 (approx.) A1 for positive y-intercept
10(b)	Correct Graph with second intersection with other graph (if correct) below <i>x</i> -axis	2	M1 for correct shape
10(c)	6.18 or 6.175 159 or 158.5 to 158.6 320 or 320.3 to 320.4	3	B1 for each
11(a)(i)	275	1	
11(a)(ii)	2.5 oe	2	<b>M1</b> for 275 ÷ 110

© UCLES 2017 Page 6 of 7

Question	Answer	Marks	Partial Marks
11(b)	09 00 oe	3	B2 for 1 h 42 mins or 102 mins soi or M1 for 170 ÷ 100 oe If 0 scored, SC1 for correct conversion of <i>their</i> decimal time into hours and mins
11(c)	24.6 or 24.63	3	M2 for $\frac{215}{12.5} \times 1.432$ or M1 for $\frac{215}{12.5}$ or $215 \times 1.432$ or $\frac{1.432}{12.5}$ soi
11(d)(i)	$\frac{325}{90+x} - \frac{110}{30+2x} = \frac{3}{2} \text{ oe}$	M2	or <b>M1</b> for $\frac{325}{90+x}$ or $\frac{110}{30+2x}$
	650(30 + 2x) - 220(90 + x) = 3(90 + x)(30 + 2x) oe	M1	Dependent on first equation containing the three terms.  Correctly eliminating fractions
	Correct completion to $x^2 - 75x + 1400$ with no errors or omissions	A2	<b>B1</b> for $2700 + 180x + 30x + 2x^2$ soi
11(d)(ii)	125 and 130	3	B2 for one or for 35 and 40 or B1 for 35 or 40 or M1 for $\frac{-(-75) \pm \sqrt{(-75)^2 - (4)(1)(1400)}}{2 \times 1}$ or sketch of parabola with two positive zeros or $(x-35)(x-40)$