

Mark Scheme (Results)

Summer 2021

Pearson Edexcel International Advanced Level In Statistics S1 Paper WST01/01

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL IAL MATHEMATICS General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- Where a candidate has made multiple responses <u>and indicates which response they</u> wish to submit, examiners should mark this response.
 If there are several attempts at a question which have not been crossed out, examiners should mark the final answer that is the <u>most complete</u>.
- 7. Ignore wrong working or incorrect statements following a correct answer

Question Number	Scheme	Marks
1. (a)	Fitst Counter Second Counter Red 37 Blue 11 37 Blue 12 7 Yellow 31 Blue 37 12 8 10 12 7 Red 12 8 10 12 7 Yellow	B1 B1
(b)	$P(Y) = \frac{7}{12} \times \frac{2}{11} + \frac{3}{12} \times \frac{2}{11} + \frac{2}{12} = \left\{ \frac{42}{132} \text{ or } \frac{7}{22} \right\} \underline{\text{or}}$ $P(\text{Yellow and two counters}) = \frac{7}{12} \times \frac{2}{11} + \frac{3}{12} \times \frac{2}{11} = \left\{ \frac{20}{132} \text{ or } \frac{5}{33} \right\}$	(2) M1
	$\frac{P([Y \cap R] \cup [Y \cap B])}{P(Y)} = \frac{\frac{20}{132}}{\frac{42}{132}}$	M1
	$=\frac{20}{42} \underline{\text{or}} \frac{10}{21} \text{oe}$	A1 (3) [5 marks]
	Notes	
(a)	1^{st} B1 for the remaining probs on first set of branches and at least one on 2^{nd} 2^{nd} B1 for a fully correct tree diagram with all the correct probabilities	set
(b)	1 st M1 for a correct ft expression for P(<i>Y</i>) or P(Yellow and two counters)ft their tree diagram eg $1 - \frac{7}{12} \times \frac{6+3}{11} - \frac{3}{12} \times \frac{7+2}{11}$ NB: The method is implied by the numbers in curly brackets but we do not need to see them to award the mark.	
	 2nd M1 for a correct ratio formula (symbols or words) and at least one correct fully correct ft ratio. Do not follow through probabilities > 1 or < 0 A1 for 10/21 or exact equivalent. (Allow 0.476190) NB if an exact correct fraction is not given and an awrt 0.476 is given by the first of the firs	
	get M1M1A0 if from correct working Generally if the answer is correct then award full marks (unless from incorrect working) or notes indicate otherwise	obvious

Questi Numb		Scheme	Mark	KS
	(a)	B and C	B1	
	(b)	A and C independent gives:		(1)
	(0)	P(C)×0.65 = 0.13 or $0.65 \times (r+0.13) = 0.13$ or $0.65 \times (0.48 - s) = 0.13$	M 1	
		P(C) = 0.2 or $r + 0.13 = 0.2$ or $0.48 - s = 0.2$	A1	
		r = 0.2 - 0.13 = 0.07 or $s = 0.48 - 0.2 = 0.28$	A1	
		P(A) + r + s = 1 or $0.65 + "0.07" + s = 1$ or $0.65 + "0.28" + r = 1$	M1	
		$s \{= 1 - 0.72 =\}$ <u>0.28</u> and $r \{= 1 - 0.93 =\}$ <u>0.07</u>	A1	(5)
	(c)	$P[(B \cup C)] = "0.2" + q \text{ or } 0.13 + "0.07" + q$	B1ft	(5)
		$P(A \cap C') = p + q \{= 0.52\}$	B1	
		$\left\{ \mathbf{P} \Big[(A \cap C') \cap (B \cup C) \Big] = q \Longrightarrow \right\} "(p+q)" \times "(0.2+q)" = q \text{ or}$		
		$"(p+q)" \times "(0.13 + "0.07" + q)" = q \text{ or } "(p+q)" \times "(1-s-p)" = 0.52 - p$	M1	
		$(p+q) \times (0.15 + 0.07 + q) = q \text{ or } (p+q) \times (1-3-p) = 0.52 - p$ [Using $p+q = 0.52$] $0.52 \times "(0.2+q)" = q \text{ or } 0.52(0.72-p) = 0.52 - p$	N/1	
			M1	
		$q = \frac{13}{60}$	A1	
		91		
		$p = \frac{31}{300}$	A1	
			F10	(6)
	(a)	Notes B1 B and C seen. If they include A then B0	[12 mar	KS
	(b)	1^{st} M1 for a correct equation for P(C) using independence.		
	(0)	1^{st} A1 for $P(C) = 0.2$ correct linear equation for <i>r</i> or <i>s</i>		
		$2^{nd} A1$ for either $r = 0.07$ or $s = 0.28$		
		2^{nd} M1 for using $\sum p=1$ Allow letter <i>r</i> and <i>s</i> or their values for <i>r</i> and <i>s</i> prov	ided they a	re
		probabilities.	nded mey d	
		3^{rd} A1 for both $s = 0.28$ and $r = 0.07$		
		NB: The quotations around the 0.07 ("0.07") imply that we ft their va	alue	
	(c)	1 st B1ft for an expression (in q) for $P(B \cup C)$ ft their value of r or their "0.2"	1	
		eg 0.13 + "their r " + q Implied by 1 st or 2 nd M1 below.		
		2 nd B1 for a correct expression for $P(A \cap C')$ in terms of <i>p</i> and <i>q</i> or 0.52 Implied by 1 st or 2 nd M1below		
		1^{st} M1 for a correct use of independence (ft their probabilities), values or let	ters.	
		Implied by 2 nd M1		
		2^{nd} M1 using $p + q = 0.52$ to gain a linear equation in one variable		
		1 st A1 for a correct fraction for q 2 nd A1 for a correct fraction for p		7
		2 ⁻⁴ A1 for a correct fraction for p SC: If both p and q are given as equivalent	0.07 C	
		recurring decimals award A0A1 eg 0.216 and 0.303		
			0.28	

Question Number	Scheme	Marks
3 (a)	Width = 2.5 (cm)	B1
	1.5 cm ² for freq of 5 so $6 \times 1.5 = 9$ cm ² for freq of 30 or fd $= \frac{5}{3}$ w $\times h = 9$	M1
	So $h = 9 \div 2.5$ or $6 \div \frac{5}{3} = 3.6$ (cm)	A1
		(3)
(b)	$Q_2 = [12] + \frac{16}{25} \times 3$ allow use of $(n + 1)$ giving $[12] + \frac{16.5}{25} \times 3$	M1
	= 13.92 = awrt <u>13.9</u>	A1 (2)
(c)(i)	$\sum fx = 5 \times 6.5 + 13 \times 9 + 16 \times 11 + 25 \times 13.5 + 30 \times 17.5 + 11 \times 24 = 1452$	M1
	$\overline{x} = 14.52 = $ awrt <u>14.5</u>	A1
(ii)	$\sum fx^2 = 6.5^2 \times 5 + 9^2 \times 13 + 11^2 \times 16 + 13.5^2 \times 25 + 17.5^2 \times 30 + 24^2 \times 11 = 23280$	(2) M1
		M1
	$\sigma_x = \sqrt{\frac{"23280"}{100} - ("14.52")^2} \underline{\text{or}} \sqrt{21.9696}$	
	$\sigma_x = 4.687 = $ awrt 4.69	A1 (2)
(d)	$\frac{1}{2} \times 13 + 16 + 25 + 30 + \frac{1}{4} \times 11$	(3) M1
(u)	$_{2}$ ×13 + 10 + 23 + 30 + $_{4}$ ×11 So proportion is 80.25 % or 0.8025 awrt 0.803	A1
	50 proportion is 00.23 % of 0.0023 uwit <u>0.002</u>	(2)
(e)	Profit = $2.2 \times "0.8025" + 0.8 \times \frac{0.75 \times 11}{100} - 1.2 \times "\left(1 - \left[0.8025 + \frac{0.75 \times 11}{100}\right]\right)"$	M1
	= 1.6935 awrt <u>1.7 (p)</u>	A1 (2)
	Notes	[14 marks]
(a)	B1 for width = 2.5 (cm) for sight of 0 cm ² or $w > h = 0$ or fd $= \frac{5}{2}$ (0.0)	
	M1 for sight of 9 cm ² or $w \times h = 9$ or fd $= \frac{5}{3}$ (o.e.) A1 for height = 3.6 (cm)	
(b)		
(~)	M1 for $\frac{16}{25} \times 3$ or $\frac{9}{25} \times 3$ or $\frac{m-12}{15-m} = \frac{16}{9}$	
	For any correct equation leading to Q_2 or correct fraction as part of Q_2	
	A1 for awrt 13.9 (use of $(n + 1)$ giving $13.98 = awrt 14.0$)	
(c)(i)	M1 for attempt at Σfx with at least 3 correct terms or $900 < \Sigma fx < 1800$	
	for info $\Sigma fx = 32.5 + 117 + 176 + 337.5 + 525 + 264$ A1 for awrt 14.5 (correct answer only 2/2)	
(ii)	1^{st} M1 for attempt at Σfx^2 with at least 3 correct terms or $20000 < \Sigma fx^2 < 26000$	000
	for info Σfx^2 = 211.25 + 1053 + 1936 + 4556.25 + 9187.5 + 6336	
	2^{nd} M1 for a correct expression including $\sqrt{(\text{ft their }\Sigma fx^2)}$ if clear it is Σfx^2) Do	not allow
	$(\Sigma f x)^2$ for $\Sigma f x^2$	
	A1 for awrt 4.69 (allow $s = 4.7107$ awrt 4.71) (correct answer only 3/	
(d)	M1 for attempt at a correct expression (allow 1 error or omission) $eg100 - \left($	$5 + \frac{13}{2} - \frac{33}{4}$
	A1 for awrt 80.3% or 0.803	·
(e)	M1 for a correct expression ft their 0.8025 o.e. eg	
	$[2.2 \times (100 - 11.5 - 8.25) + 0.8 \times 8.25 - 1.2 \times 11.5] \div 100$	
	Condone $[2.2 \times "80" + 0.8 \times (8) - 1.2 \times (12)] \div 100$	
	A1 for awrt 1.7 Allow £0.017 (this must have units)	

Question Number	Scheme	Marks
4. (a)	$P(W < 120) = P\left(Z < \frac{120 - 165}{35}\right)$	M1
	$= P(Z < -1.2857) = 1 - 0.9015 \text{ or } 1 - 0.9007285$ $= 0.09927 = awrt 0.0985 \sim 0.0994$	M1 A1 (3)
(b)	e.g. $P(W > x) = \frac{1}{3}$ gives $\frac{x - 165}{35} = \pm 0.43$ (calculator 0.430727)	M1B1
	Limits 149.9245 to 180.0754 awrt <u>150</u> to <u>180</u>	A1, A1 (4)
(c)	$P(W < 200 W > "180") \underline{\text{or}} \frac{P("180" < W < 200)}{P(W > "180") \text{or} \frac{1}{3}}$	M1
	$=\frac{0.8413(44739)-\frac{2}{3}}{\frac{1}{3}}$	A1 (num)
	= 0.52403 <u>(0.523~0.5264)</u>	A1 (3)
(d)	$\frac{1}{3} \times \frac{1}{3} \times \frac{1}{3}; \times 3!$	M1;M1
	$\frac{1}{3} \times \frac{1}{3} \times \frac{1}{3}; \times 3! = \frac{2}{9}$	A1
		(3)
	Notes	[13 marks]
(a)	1^{st} M1for standardising with 120 (allow 210), 165 and 35. Accept \pm 2^{nd} M1for attempting $1 - p$ [where $0.85]A1for awrt 0.0985~0.0994 (Correct ans only 3/3)$	
(b)	M1 for standardising with x (o.e.) 165 and 35 and setting equal to a z value, (Accept $\frac{165-x}{35} = \pm z$ where $0.4 < z < 0.5$)	0.4 < z < 0.5
	B1 for use of $z = 0.43$ or better We must see 0.43 or better. 1 st A1 for lower limit of awrt 150 2 nd A1 for upper limit of awrt 180	
SC	A0A1 for two limits symmetrically placed about 165 provided M1 scored NB: correct answers with no working can score M1B0A1A1	
(c)	M1 for a correct probability statement (either form) ft their 180 or a correct ratio $1^{st} A1$ for a correct numerator (awrt 0.175)	
	2 nd A1 for an answer in the range awrt 0.523~0.5264 (use of 180 gives 0.5263)	8869)
(d)	1 st M1 for $\left(\frac{1}{3}\right)^3$ (or equivalent)	
	2^{nd} M1 for $p \times 3!$ (or equivalent) where 0	
	A1 for $\frac{2}{9}$ or any exact equivalent	

Question Number	Scheme	Marks
5. (a)	{E(X) = } $-2a - b + 0 \times c + b + 4a$ or $2a$ { $2a = 0.5$ so } <u>$a = 0.25$</u>	M1 A1
(b)	{ $E(X^2) = \{(-2)^2 \times a + (-1)^2 \times b + 0 + 1^2 \times b + 4^2 \times a \text{ or } 20a + 2b \text{ (o.e.)} $ { $Var(X) = \}^{"}20a + 2b" - 0.5^2$ 20a + 2b - 0.25 = 5.01 (o.e.) e.g. "4.75" + 2b = 5.01 { $2b = 0.26 \text{ so } \} $ b = 0.13 { Use of sum of probs = 1 to calculate a 2 nd value } c = 0.24	(2) M1 M1 A1 A1 A1ft
(c)(i) (ii)	{E(Y) = 5 - 8×0.5 } = <u>1</u> {Var(Y) =} (-8) ² ×5.01 = 320.64 awrt <u>321</u>	(5) B1 M1 A1
(d)	$4X^{2} > 5 - 8X$ $(2X - 1)(2X + 5) > 0 \implies X > 0.5$ So need X = 1 or 4 <u>or</u> probability of $a + b$ $= \underline{0.38}$	(3) M1 M1A1 M1 A1
		(5) [15 marks]
(a)	NotesM1for any correct expression for $E(X)$ in terms of a (or a, b, c)A1for $a = 0.25$	
(b)	1^{st} M1for attempt at an expression for $E(X^2)$ with at least 3 correct non-zero terms 2^{nd} M1for a correct expression for $Var(X)$ eg" $18a - c + 1" - 0.5^2$ Allow with their value $0f$ a substituted 1^{st} A1for a correct equation for b (or possibly c) eg" $18a - c + 1" - 0.5^2 = 5.01$ Allow 1^{st} A1for either value of a substituted 2^{nd} A1for either $b = 0.13$ or $c = 0.24$ 3^{rd} A1ftfor using $c = 1 - 2 \times "0.25" - 2 \times "0.13"$ or $b = (1 - 2 \times "0.25" - "0.24") \div 2$ to gain	
(c)	B1 for $\{E(Y) =\} 1$ M1 for correct use of $Var(aX + b) = a^2 Var(X)$ A1 for awrt 321	
(d)	1^{st} M1for correct quadratic inequality (may be inside prob statement) of 2^{nd} M1for an attempt to solve or identifying correct X values 1^{st} A1for $X > 0.5$ [may also have $X < -2.5$] 3^{rd} M1for realising need $X = 1$ and 4 only or answer of their $(a + b)$ 2^{nd} A1for 0.38 (or exact equivalent) only (correct ans only 5/5)	or table of values

Question Number	Scheme	Marks
6. (a)	$\left\{\mathbf{S}_{yy} = \right\} 42.63 - \frac{23.7^2}{16} = [7.524375]$	B1
		(1)
(b)	Use of $\overline{y} = 3.684 - 0.3242\overline{x}$; so $\sum x = 16 \times \left(\frac{3.684 - \frac{23.7}{16}}{0.3242}\right) = 108.71067.$	M1; A1
	$\{S_{xx} =\}756.81 - \frac{("108.71")^2}{16}; = 18.18435 \text{ awrt } \underline{18.2}$	M1; A1
	S	(4)
(c)	$b = \frac{\mathbf{S}_{xy}}{\mathbf{S}_{xx}} \Longrightarrow \mathbf{S}_{xy} = "18.1843" \times (-0.3242) [= -5.8953]; \ r = \frac{"-5.89536"}{\sqrt{"18.184" \times 7.524375}} = -0.50399 = -0.49 \sim -0.51$	M1; M1
	$= -0.50399 = -0.49 \sim -0.51$	A1
(d)	Sub $x = 2$ in the regression line gives $y = 3.0356$	(3) B1
		(1)
(e)	St.dev = $\sqrt{\frac{S_{xx}}{n}} = \sqrt{\frac{"18.184"}{16}} = 1.066$	M1
	So limits are: $\frac{"108.71"}{16} \pm 3 \times "1.066" = 3.5965~ 9.9929 = awrt 3.6~10$	M1, A1
	$\frac{16}{16} = 1000000000000000000000000000000000000$	
(f)	The probability of $x = 2$ being in the range is very small;	(3) B1ft;
(1)	so Behrouz's estimate is <u>unreliable</u>	dB1ft (2)
(g)	Should use regression of x on y to estimate unemployment or equivalent	B1
	So Andi's suggestion is not suitable or not to be recommended	dB1 (2)
	N. 4	[16 marks]
(a)	Notes B1 Value given so must see sight of a correct expression – allow 561.69 fr	for 23.7^2
(b)		
	1 st A1 for $\sum x = awrt 109$	
	2^{nd} M1 for a correct expression for S _{xx} ft their Σx	
	2 nd A1 for awrt 18.2	
(c)		
	2 nd M1 for a correct expression for <i>r</i> ft their S_{xy} and S_{xx} A1 for an answer in the range $-0.49 \sim -0.51$	
(d)	e	
(e)	1 st M1 for a correct attempt at st. dev. ft their S _{xx} or $\sqrt{\frac{756.81}{16} - \left(\frac{"108.71"}{16}\right)^2}$	\int_{0}^{2} ft their Σx
	2 nd M1 for one correct calcft their values	
	A1 for a range awrt $3.6 \sim 10$	an A 11 are
(f)	extrapolation	ge. Allow
	2^{nd} dB1ft dep on 1 st B1 for stating a correct conclusion for their range	1 1 1
(g)	1 st B1 for a suitable reason based on reg line, eg regression line $(y \text{ on } x)$ can to estimate wages. Allow x instead of unemployment and y instead of	•
	2 nd dB1 dep on 1 st B1 for suggesting not suitable (or equivalent)	~

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